

# Photon pressure calibrator in GEO600



*A safe and reliable method ?*

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# Photon pressure calibrator: independent check of absolute calibration

**Absolute calibration of the ESDs:  
ESDs  $\Rightarrow$  MMC2\_feedback  $\Rightarrow$  Master laser piezo**

## Potential problems:

- Many steps involved (accumulating errors)
- Some measurements have low SNR
- Some measurements are only done at certain frequencies
- longterm stability of ESDs (unknown)

Independent check of calibration using:

$$F = 2 \frac{P}{c}$$

Resulting displacement:

$$x(\omega_m) = \frac{2P_m \cos(\alpha)}{Mc\omega_m^2},$$



# A brief history of the efforts in GEO (1)

## 1st setup (February 2004)

- Laser diode (976 nm)
- poor optical setup
- ‚proof of principle‘, but deviation from  $1/f^2$  was observed.

## 2nd setup (Spring 2005)

- Fibre coupled Laser diode (1035 nm)
- Improved optical setup
- Better measurements: SNR improved by 1 order of magnitude (due to improved sensitivity of GEO600).
- Between 100 and 1000 Hz good agreement to official calibration.



# Measurements from spring 2005



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Physics Letters A 353 (2006) 1–3

PHYSICS LETTERS A

[www.elsevier.com/locate/pla](http://www.elsevier.com/locate/pla)

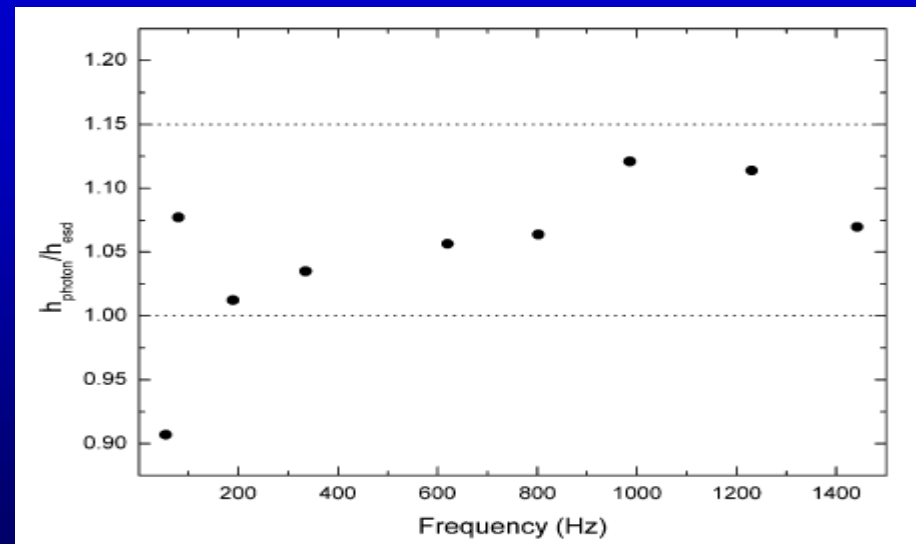
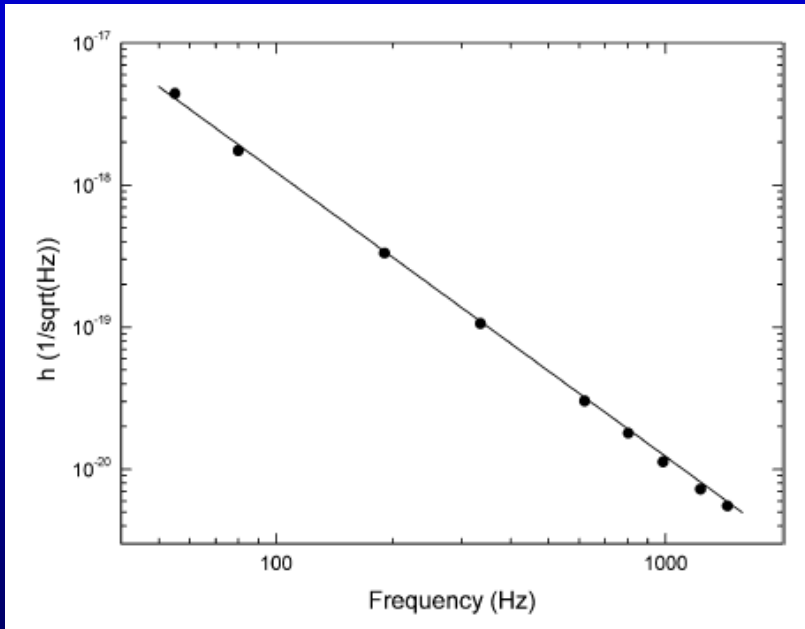
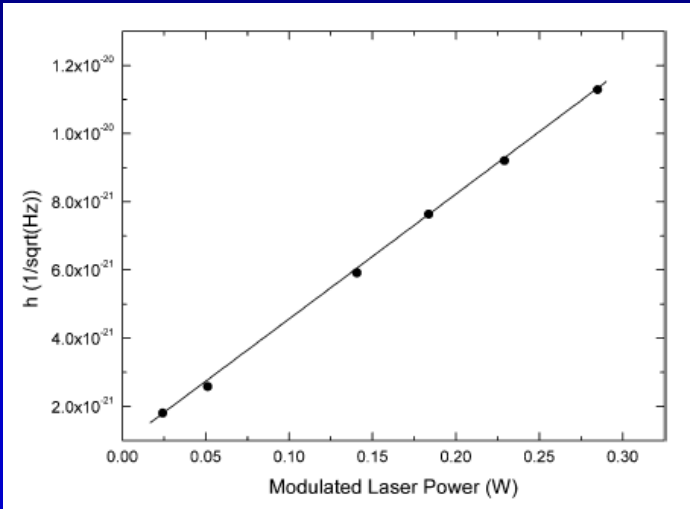
## A photon pressure calibrator for the GEO 600 gravitational wave detector

K. Mossavi\*, M. Hewitson, S. Hild, F. Seifert, U. Weiland, J.R. Smith, H. Lück, H. Grote,  
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Max-Planck-Institut für Gravitationsphysik (Albert-Einstein-Institut) und Universität Hannover, Callinstr. 38, 30167 Hannover, Germany

Received 7 November 2005; received in revised form 20 December 2005; accepted 21 December 2005

Available online 28 December 2005





## A brief history of the efforts in GEO (2)

### Accuracy achieved with 2nd setup:

- Absolute: within 15% to the official calibration.
- Relative: within +/- 8%

### 2nd setup improved (early 2006)

- Improved alignment and centering of the beam on testmass
- Improved accuracy of the power measurement.
- Measurements are done towards higher frequencies
- Continuous injecting of a calibration line for S5.

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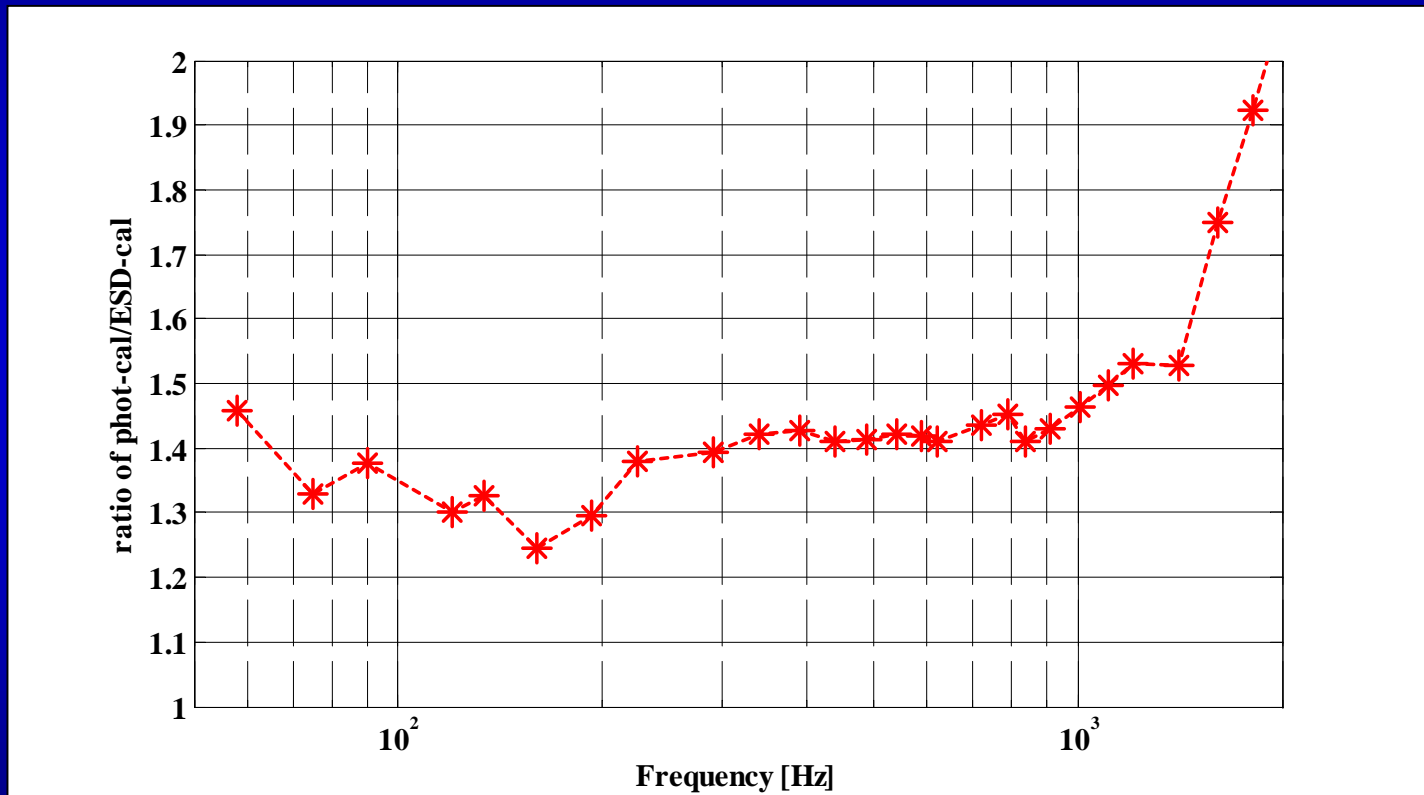
=> Observed surprisingly large discrepancy to official calibration.



# Results with present setup

What we would like to get is:

phot-cal/ESD-cal = 1



This does not work out in reality. ☹️

We observe a remarkably large discrepancy, but ...

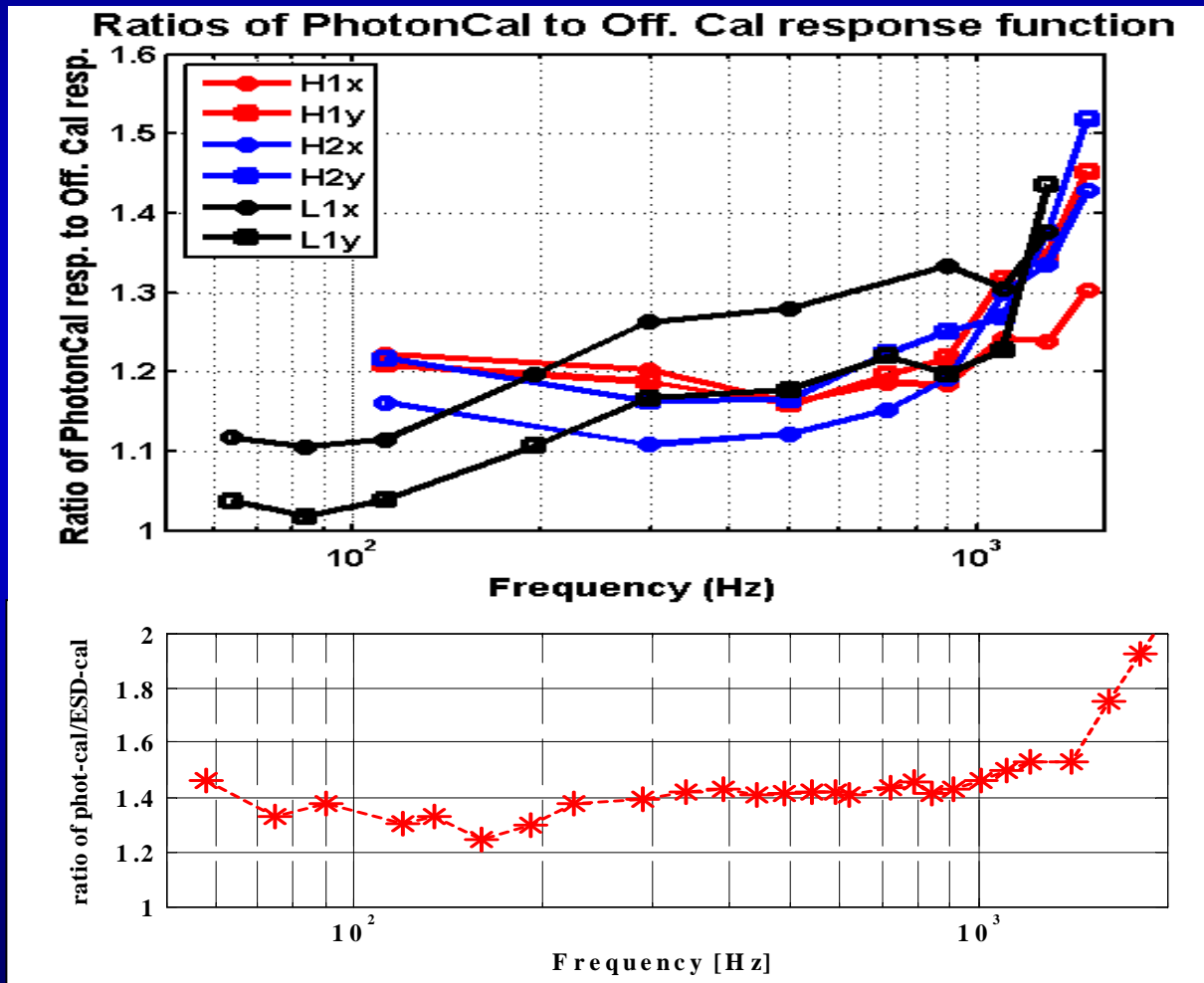


# The GEO results vs the LIGO results

Credits for the LIGO measurements:

Peter Kalmus, Evan Goetz, Rick Savage, Brian O'Reilly, Mike Landry

..., but we seem to be in good company:





# Official calibration

**It is important to state here:**

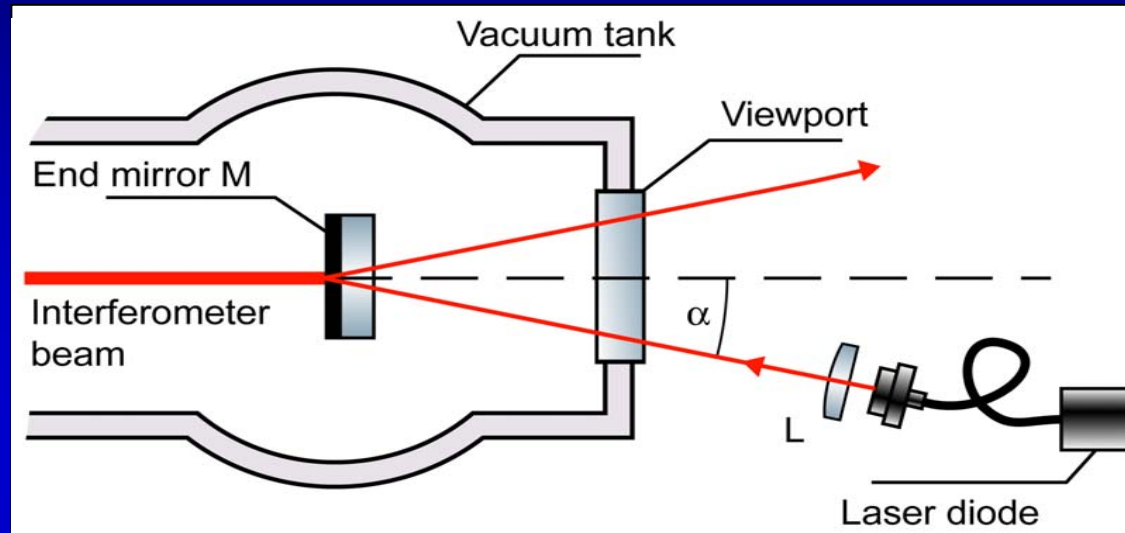
**WITHIN BOTH PROJECTS (LIGO and GEO) MANY CROSSCHECKS OF THE OFFICIAL CALIBRATIONS HAD BEEN PERFORMED.**

- **There is a high confidence level for the official calibrations.**
- **There are believed to be correct to within 10%.**
- **Both projects believe that the discrepancy originates from the photon pressure actuators being imperfect.**





# The GEO setup



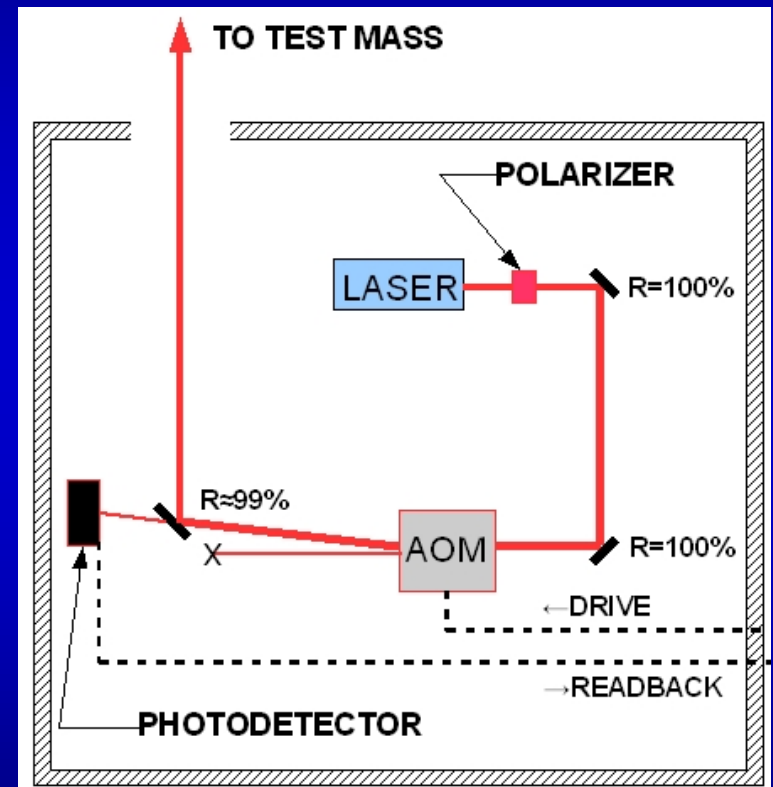
- Source: modulated Laser diode.
- Wavelength = 1035 nm, DC power = 1 W, modulated power up to 800 mW.
- Power is monitored by an photodiode inside the Laser diode.
- Shining from back (through the substrate)
- Restricted geometrical setup: the reflected beam is clipped on the way out of the vacuum.
- PPD beam diameter at MFN = 5mm (main IFO beam = 50 mm)



# The LIGO setup

Credits: Peter Kalmus, Evan Goetz, Rick Savage, Brian O`Reilly, Mike Landry

- Source: Laser + AOM.
- Wavelength = 1036, DC power = 300mW, modulated power up to 150 mW.
- Power is monitored by an photodiode in front of the vacuum.
- Shining onto the front surface of the testmass.
- Restricted geometrical setup: the reflected beam is not accessible.
- PPD beam diameter at Testmass = 10-20 mm, main IFO (H1) beam = 90 mm (ETM) *(values from pc with Keita)*

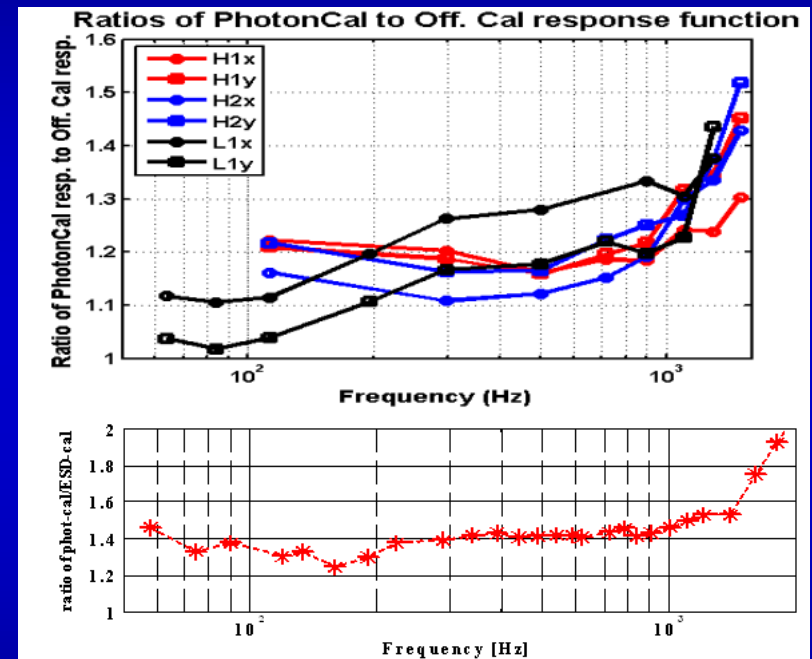




# GEO vs LIGO

Hypothesis: If the discrepancies in GEO and LIGO have the same origin we can rule out several points.

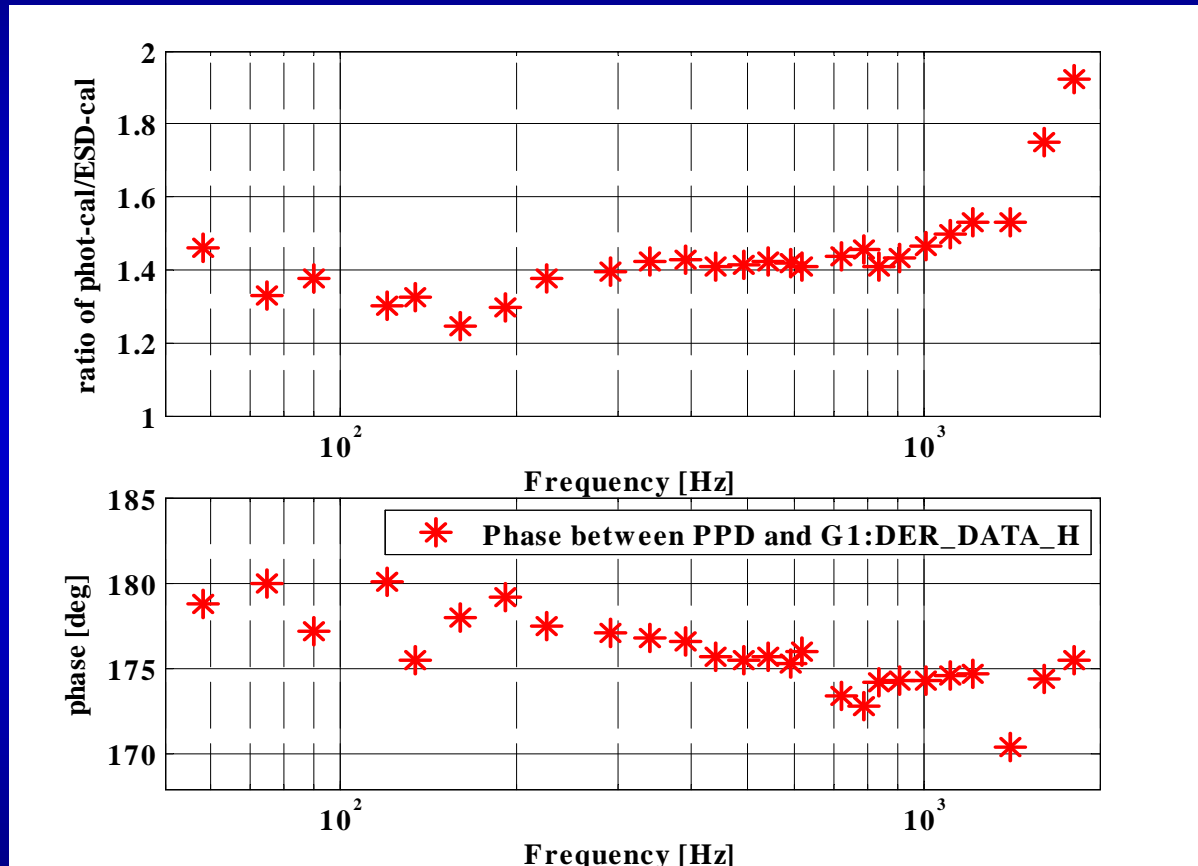
- Official calibration is different (ESD vs coil magnet, Signal-Recycling vs arm cavities, etc)  
*=> Ruling out any effects from official calibration procedures*
- LIGO shines on the front surfaces, while GEO is coming from the back through the substrate.  
*=> Ruling out any thermal effects from the mirror substrate*





# Discrepancy + Phase

The phase contains a lot of information we should include !!!

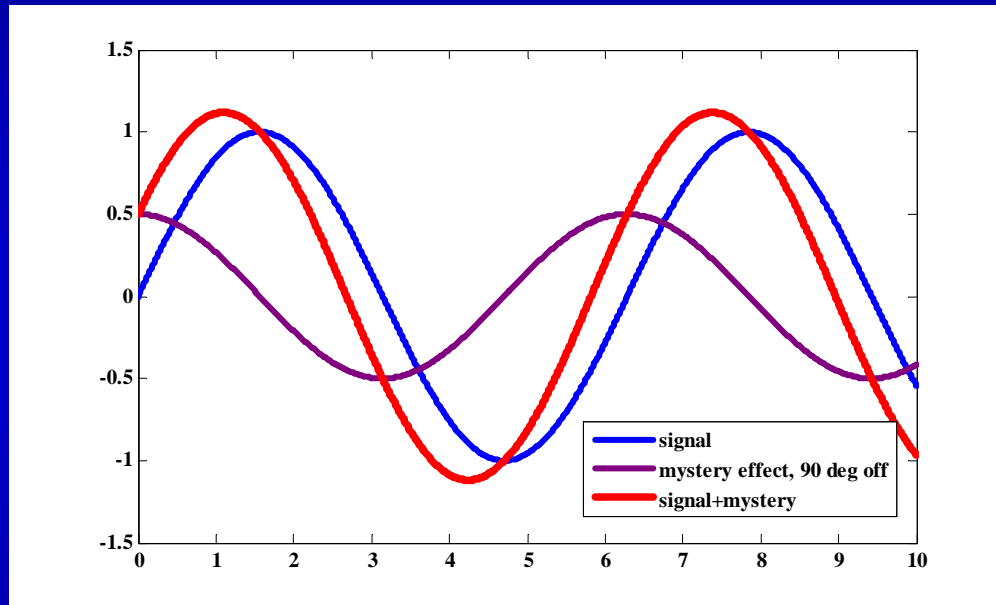


Due to the pendulum response the mirror is  $180^\circ$  out of phase with the applied light modulation (quite unintuitive).



# Phase picture

Considering a second effect („mystery“) coming into the game (thermal absorption + thermal expansion) with 90 deg different phase:



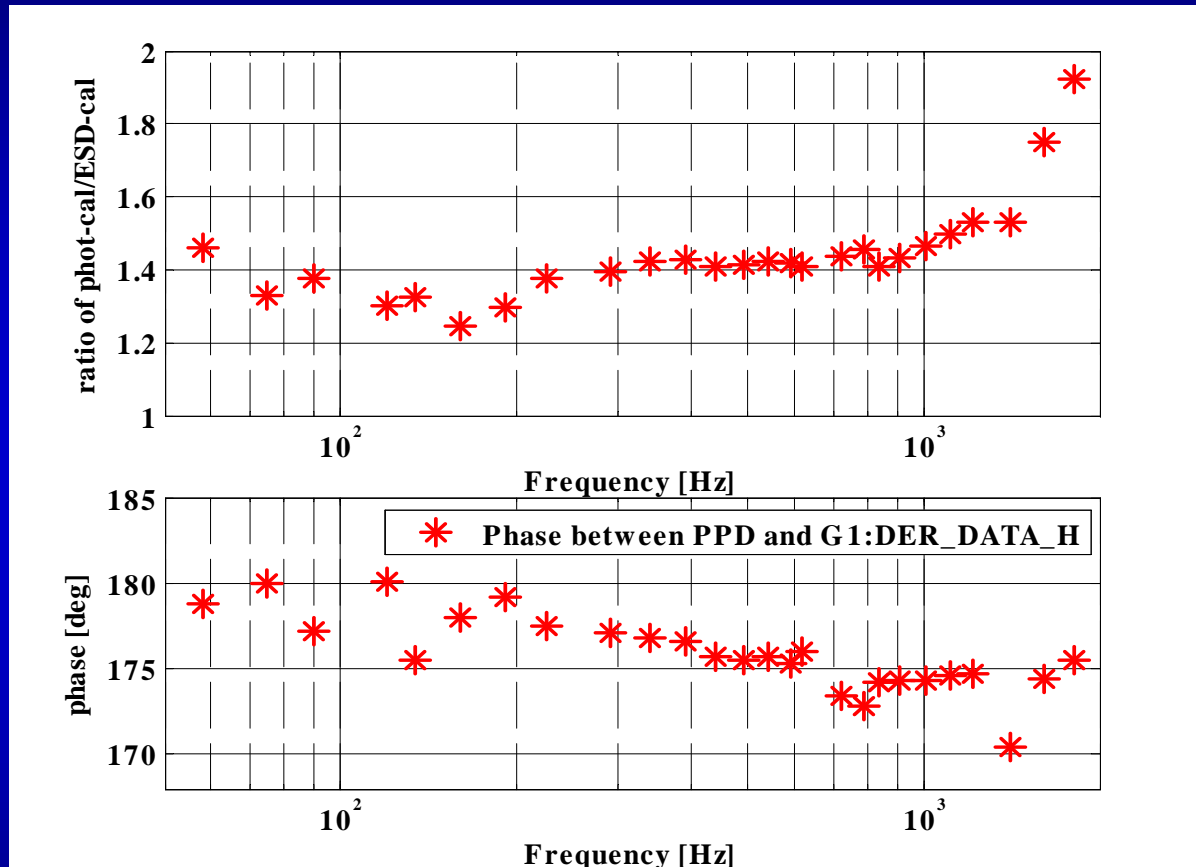
The resulting amplitude gets larger. In contrast we observe in the experiments a smaller amplitude than expected.

⇒ The mystery effect needs to have a phase between 0 and 90 deg.

⇒ There is also a phase shift due to the mystery effect.



# Discrepancy + Phase

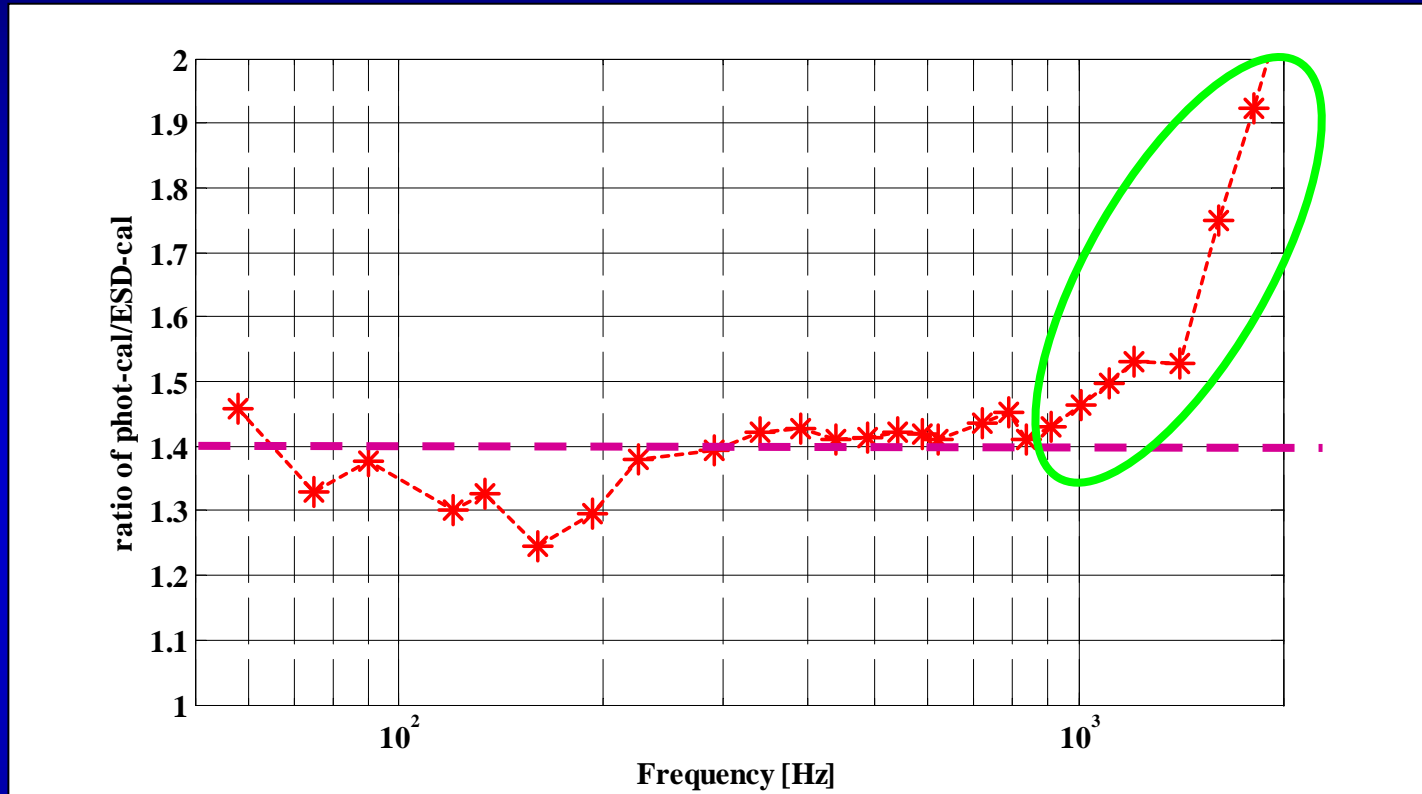


The observed phase stays at 180 deg.

**=> The mystery effect needs to have a phase near 0 deg. (if you add a 0 deg and a 180 deg effect phase stays constant, while amp changes)**



# Two main problems

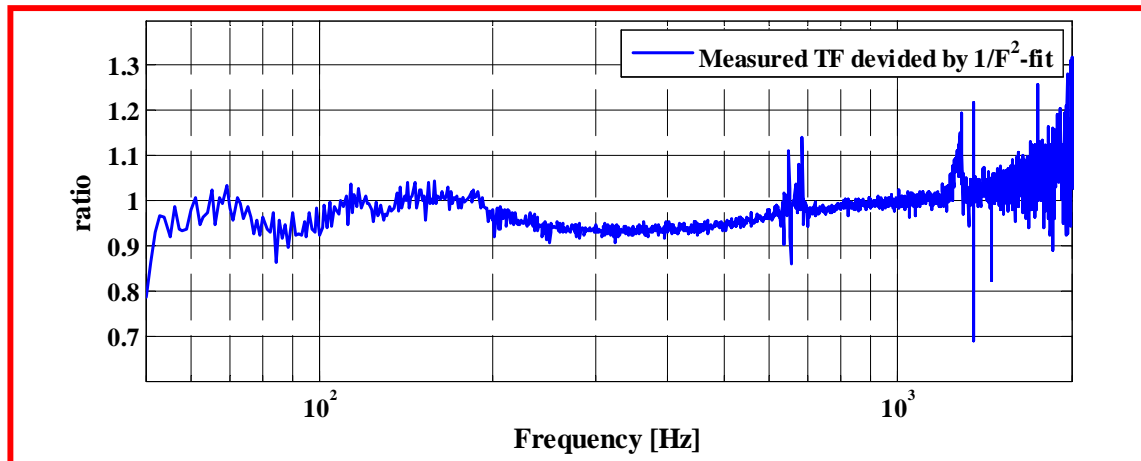
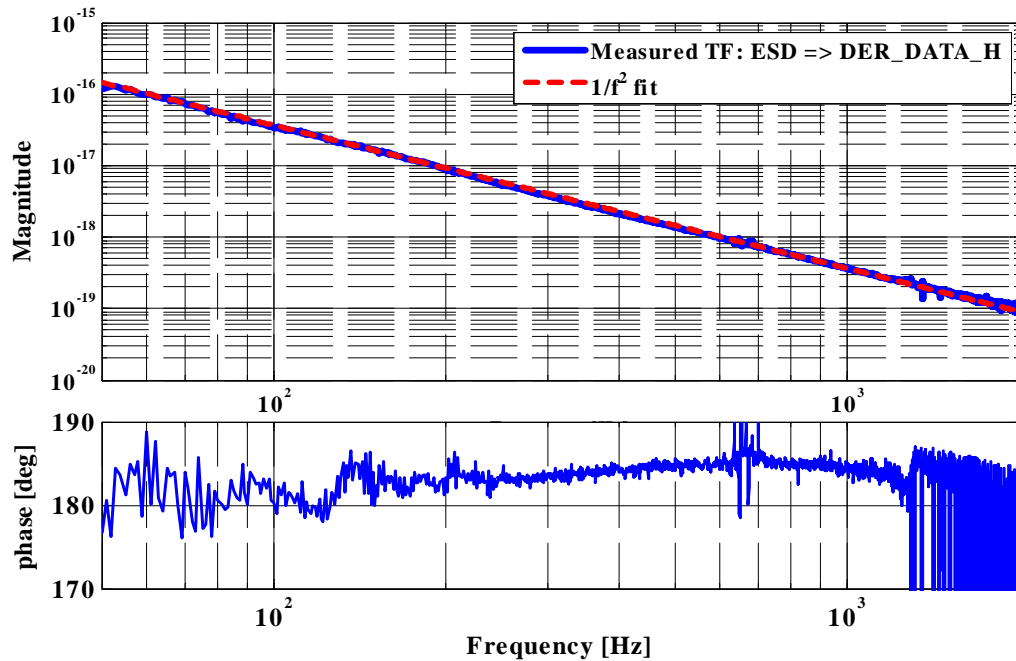


1. Absolute deviation of 40 % (amp in DER\_DATA\_H is smaller than expected)

2. Step roll off above 1kHz



# Ruling out any artefacts from calibration process: Checking the $1/f^2$ of ESD vs official calibration.



TF from ESD-FB to  
DER\_DATA\_H is  
 $1/f^2$  within +/-5%





## Brainstorming: discrepancy @ high freqs.

Assuming the monitor diode gives a correct measure of the power leaving the PPD then:

- We don't believe that the power hitting the mirror is wrong by 50%.
- Secondary effects like for instance absorption+thermal\_expansion would do with much less power-loss. (photothermal absorption)



# Photothermal absorption in the game?

JOURNAL OF APPLIED PHYSICS

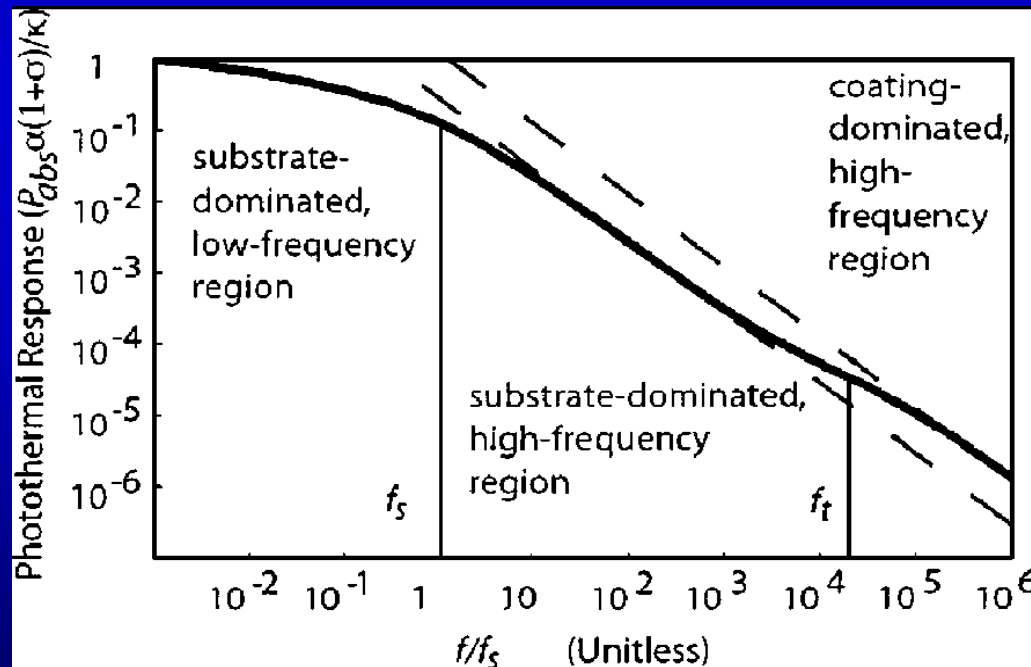
VOLUME 95, NUMBER 12

15 JUNE 2004

## Enhanced photothermal displacement spectroscopy for thin-film characterization using a Fabry-Perot resonator

Eric D. Black, Ivan S. Grudinin, Shanti R. Rao, and Kenneth G. Libbrecht  
*LIGO Project, California Institute of Technology, Mail Code 264-33, Pasadena, California 91125*

(Received 23 October 2003; accepted 5 March 2004)





## Brainstorming: discrepancy @ high freqs.

Assuming the monitor diode gives a correct measure of the power leaving the PPD then:

- We don't believe that the power hitting the mirror is wrong by 50%.
- Secondary effects like for instance absorption+thermal\_expansion would do with much less power-loss. (photothermal absorption)
- Are our mirrors really rigid bodies?

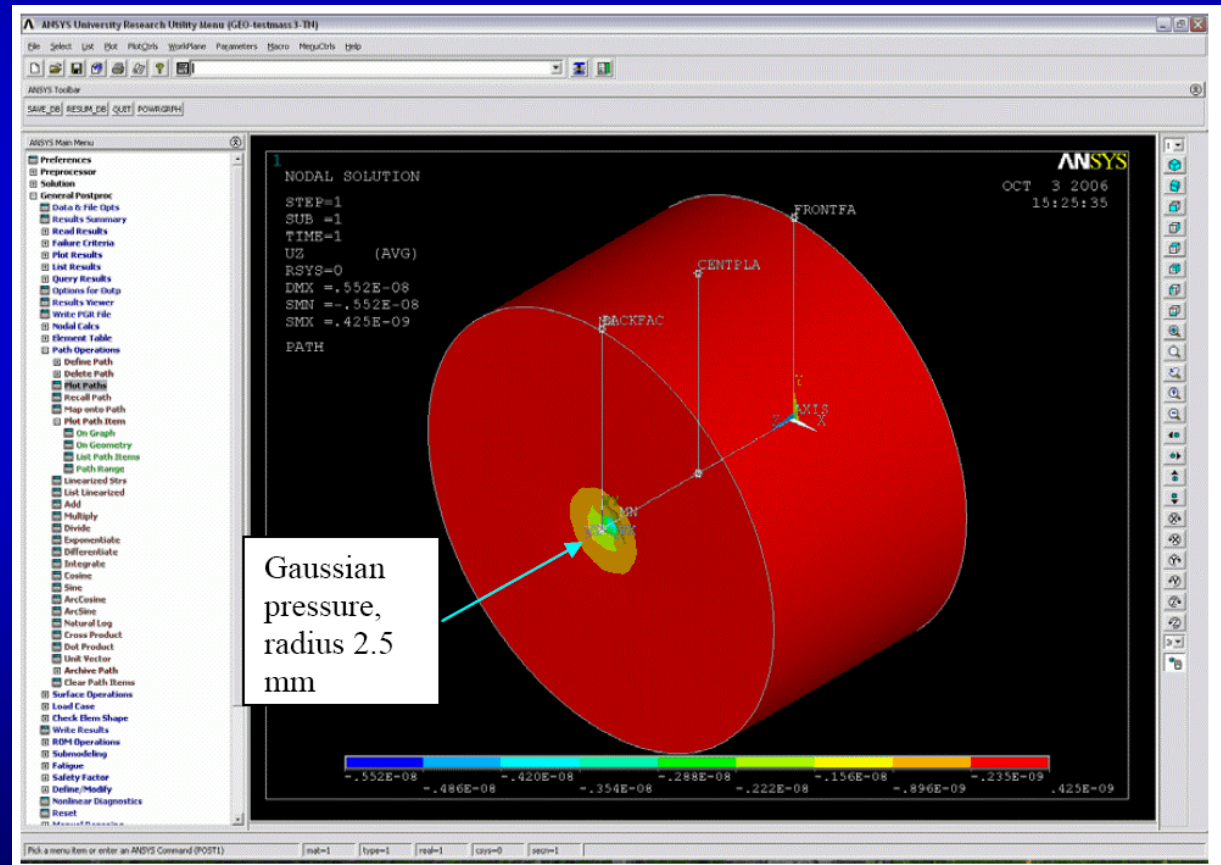


# Finite Element Simulation

Credits to Iain Martin, Stuard Reid, Jim Hough (IGR, Glasgow)

Applying a gauss shape force (2.5mm radius) of 2.77 N to the center of a GEO-mirror.

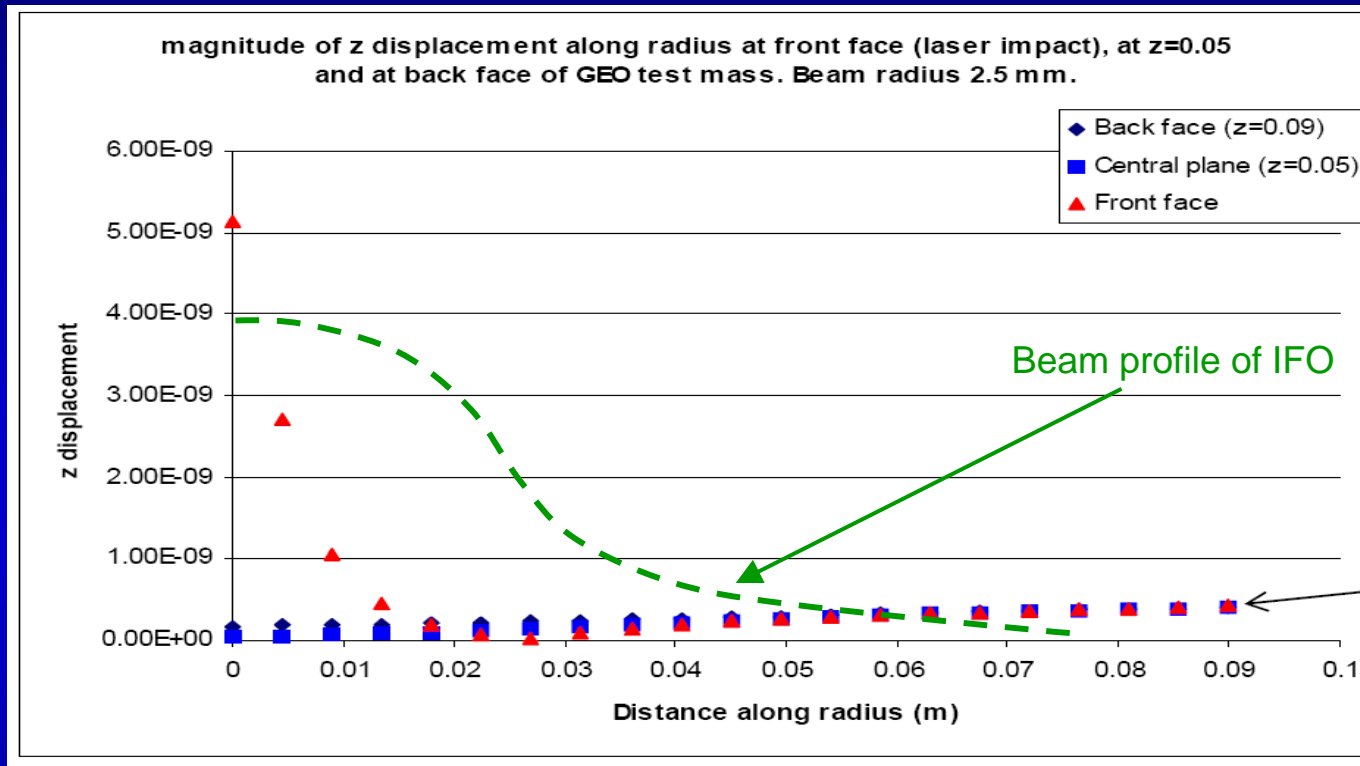
The test mass is held in place using the inertial relief function in Ansys





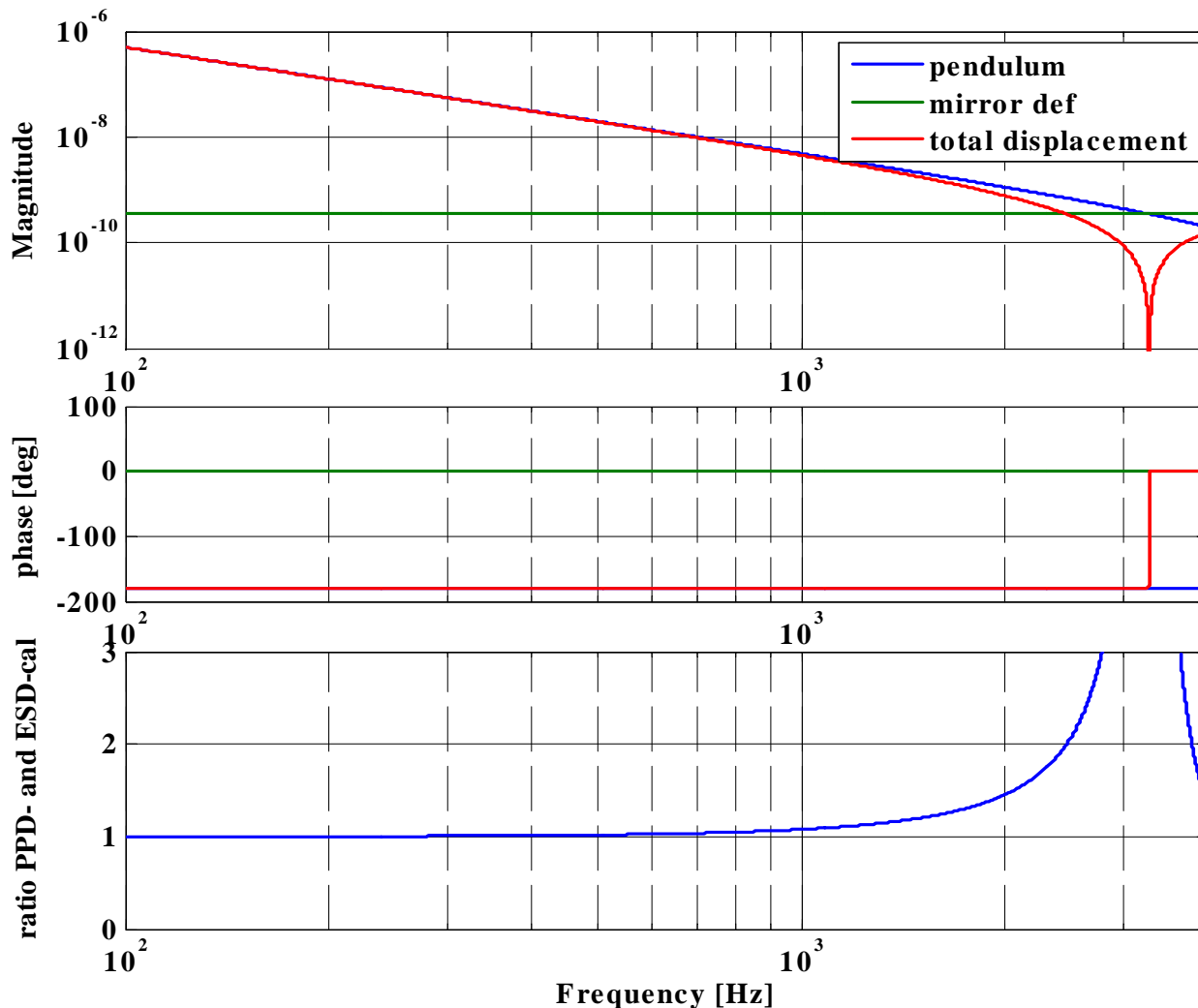
# Finite Element Simulation (2)

Credits to Iain Martin, Stuard Reid, Jim Hough (IGR, Glasgow)



- The displacement needs to be weighted by the overlap of the main IFO beam. For now I will use  $1e-9 \text{ m}/2.77\text{N}$ .
- I assume the displacement to be flat in frequency (below the resonance) and in phase with the applied light.

# Simple model (including mirror deformation)

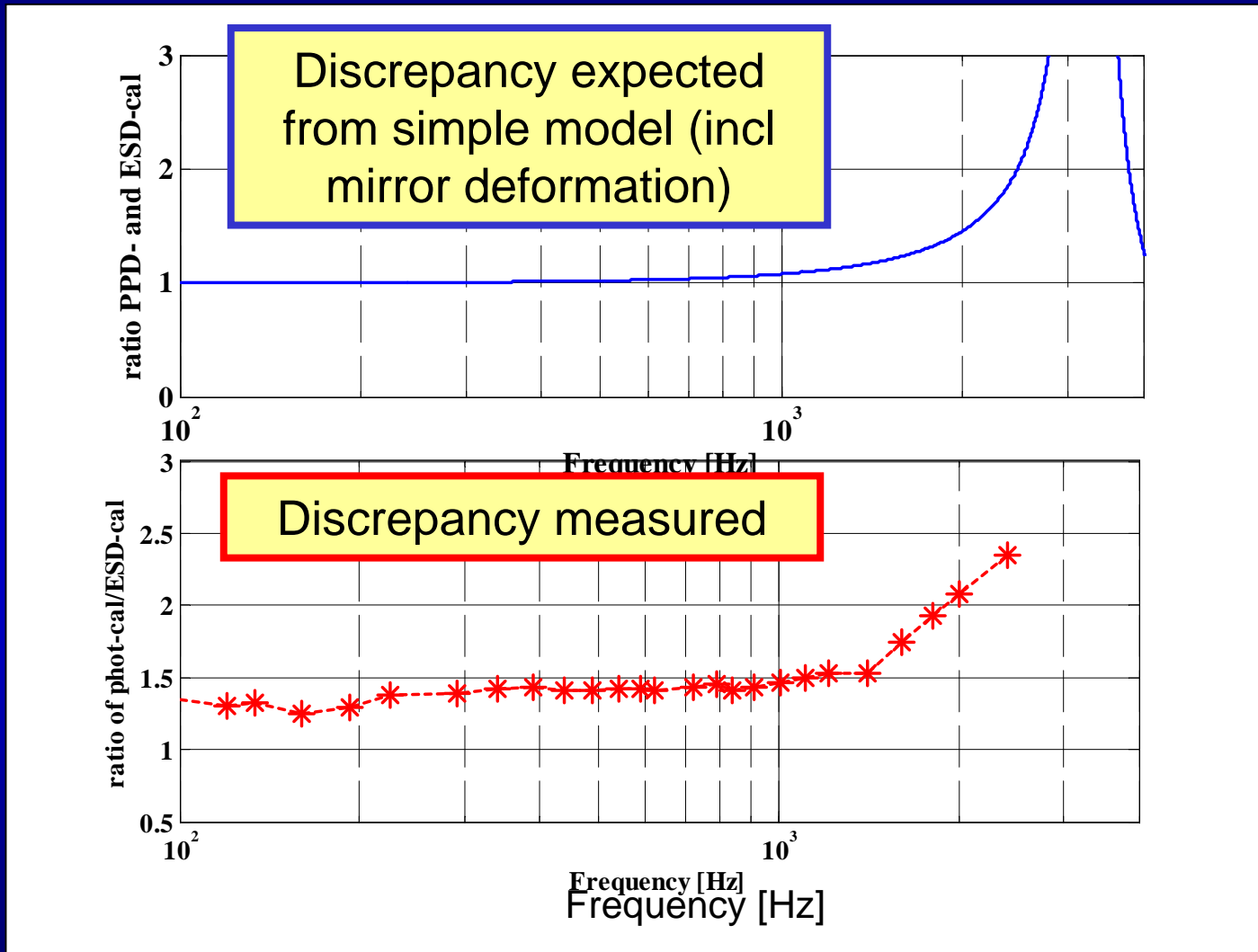


Pendulum resp:  
 $1/f^2$   
 $5e-7m/N$  at 100Hz  
 Phase =  $180^\circ$

Displacement  
 from mirror defor.:  
 flat  
 $3.6e-10m/N$   
 Phase =  $0^\circ$

Resulting  
 discrepancy

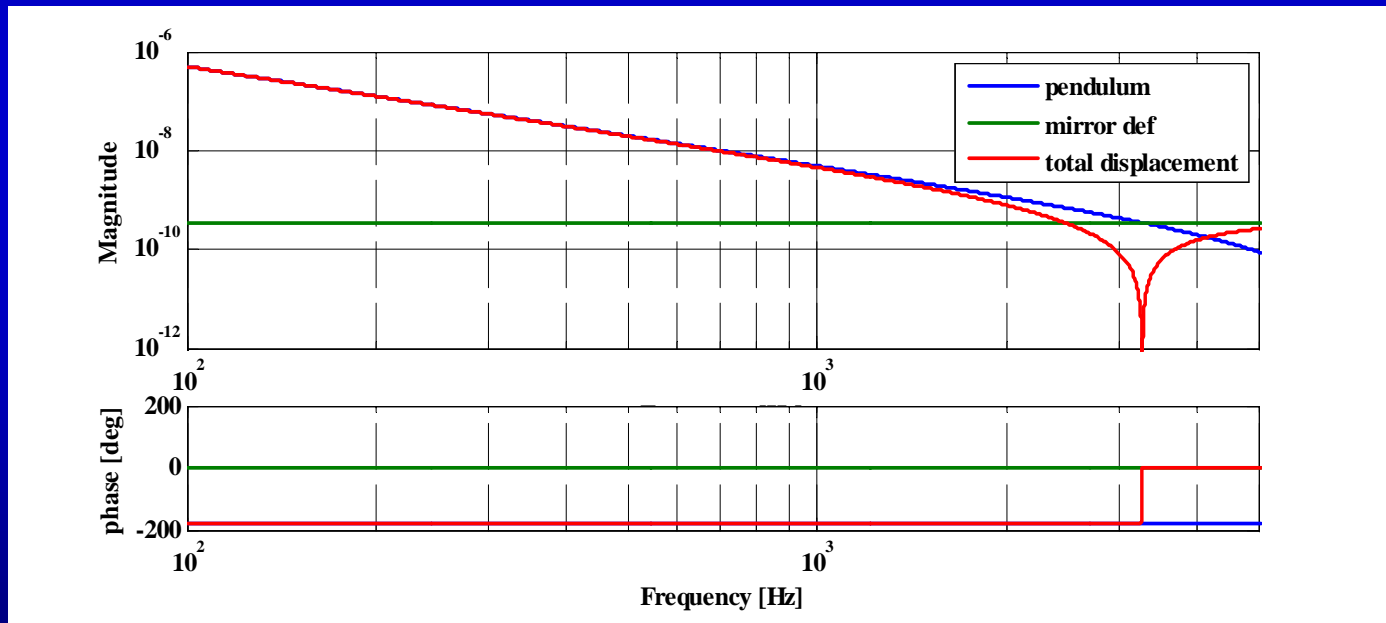
# Comparison of model and measurement





# To-Do: check simple model vs experiment

- Easiest to do by injecting a high frequency line and checking the phase (at the crossover it will jump from 180 to 0 deg).
- Amplitude response should become flat in frequency above the crossover (hard to check because of very small signal)

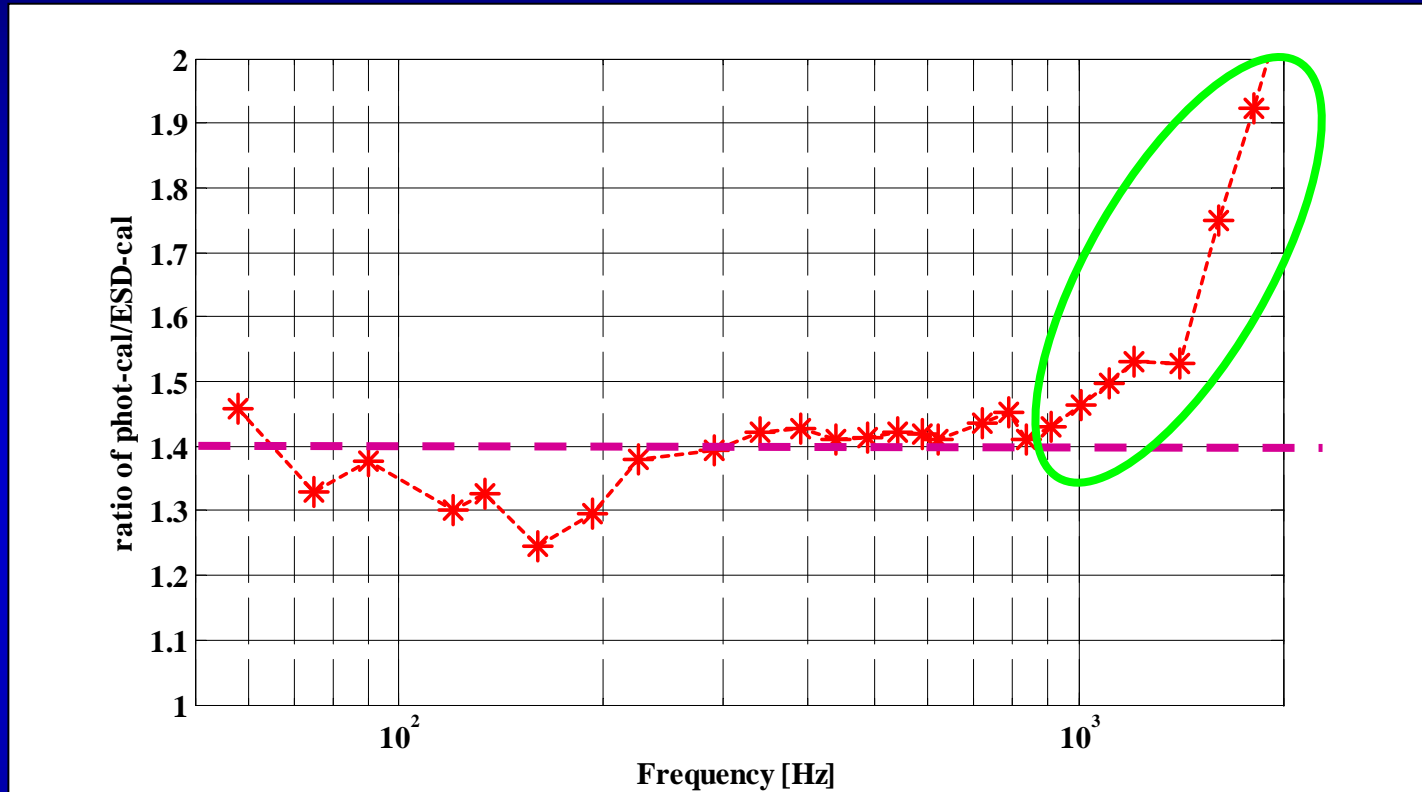


To get rid of the problem: Increase PPD beam radius @ testmass.





# Two main problems

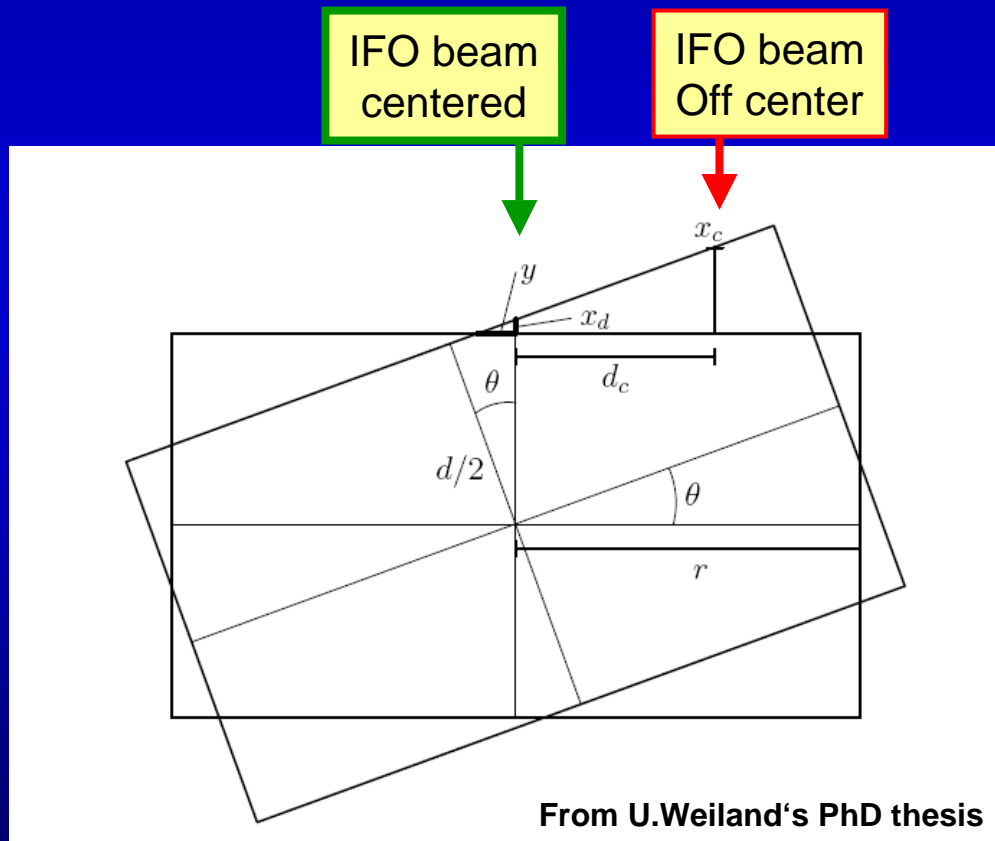


1. Absolute deviation of 40 % (amp in DER\_DATA\_H is smaller than expected)

2. Step roll off above 1kHz

# Effects from mirror rotation/tilt (yaw/pitch)

The photon pressure actuator can cause rotation (and or tilt) when hitting the mirror off center.



IFO beam centered:

$$x_d \approx \frac{d}{4} \theta^2$$

IFO beam off center:

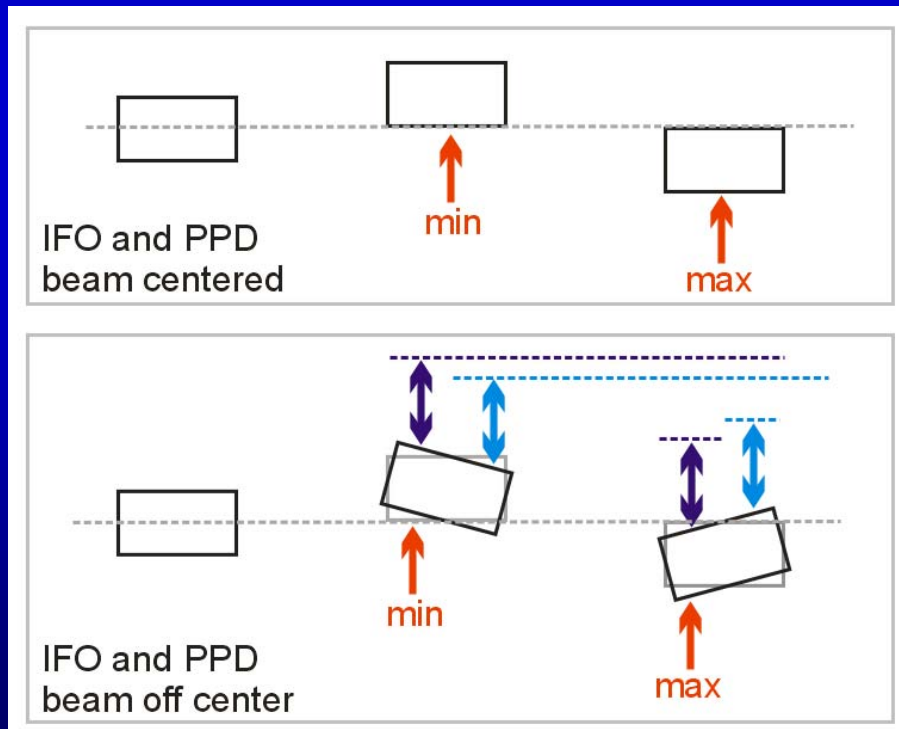
$$x_c \approx d_c \theta + \frac{d}{4} \theta^2$$



# Effects from mirror rotation in phase picture

In principle there is no difference between longitudinal and rotational pendulum response:

- resonances are far below the frequencies of interest
- both give an  $1/f^2$
- both are  $180^\circ$  out of phase to the light.



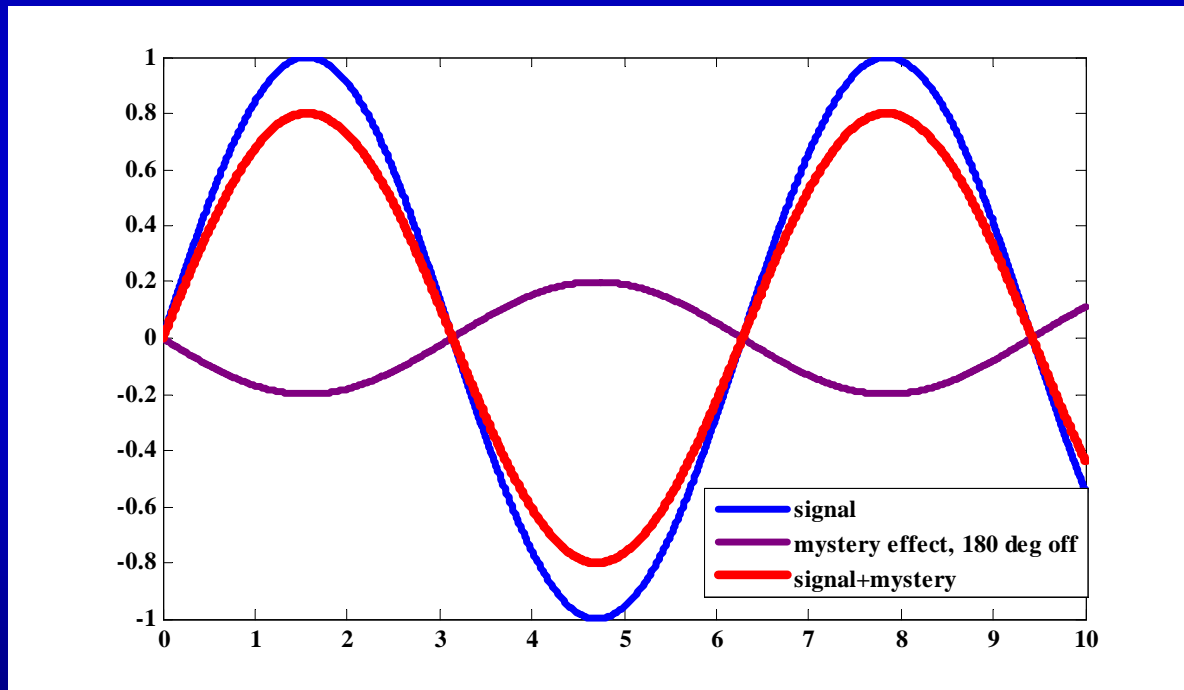
When IFO and PPD are off center to the same side:  
Rotation gives **180 deg.**

When IFO and PPD are off center to opposite directions:  
Rotation gives **0 deg.**



## Effects from mirror rotation in phase picture (2)

When IFO and PPD are off center to opposite directions:  
Rotation gives 0 deg (in respect to the light)  
Rotation gives 180 deg (in respect to longitudinal)



This effect would reduce the signal for the same amount over all frequencies !!



## Can this effect explain 40% error ?

How far would we have to off the center to explain 40% ?

Displacement from rotation

$$x_c(\omega) \approx \frac{2Pd_c d_{PPD}}{Ic\omega^2}$$

Displacement from longitudinal

$$x(\omega) = \frac{2P}{Mc\omega^2}$$

$$\frac{x_c(\omega)}{x(\omega)} = \frac{Md_c d_{PPD}}{I}$$

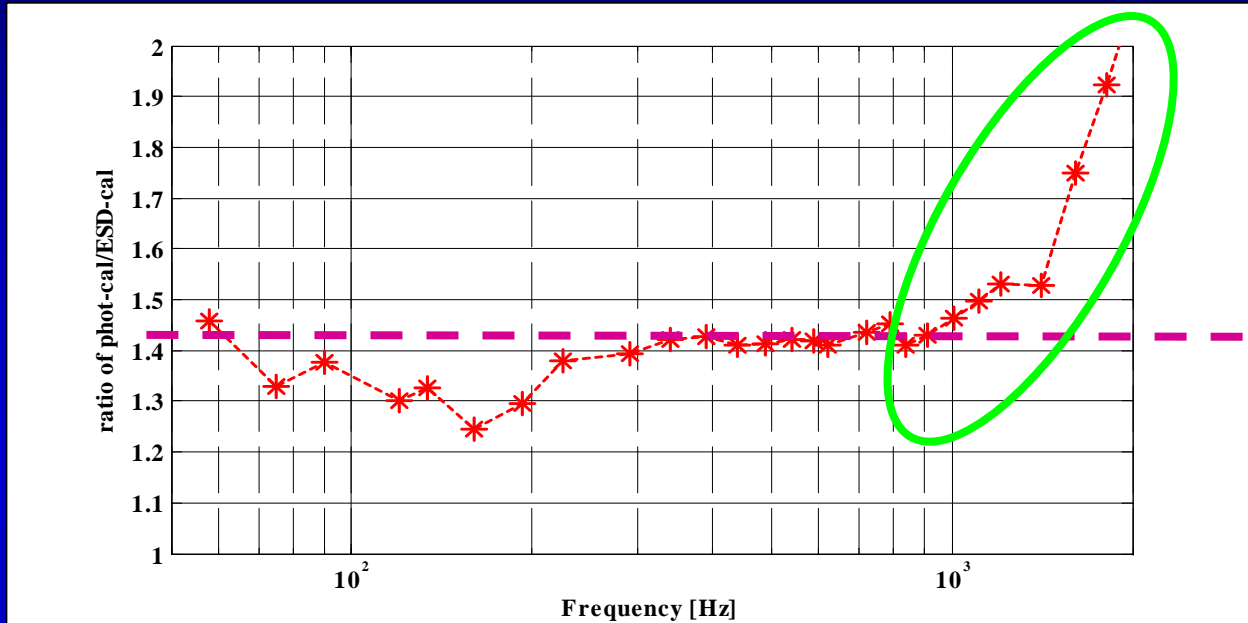
$$d_c d_{PPD} = 0.4 \frac{I}{M} = 1.21 \cdot 10^{-3} \text{m}^2 \quad d_c = d_{PPD} = 3.4 \text{cm}$$

Error of 40% corresponds to being 3.4 cm of center.

To get better 1% beams need to be centered within 0.5 cm.



# Two main problems + candidates



1. Absolute deviation of 40 % (amp in DER\_DATA\_H is smaller than expected)

**Candidate: PPD and IFO not hitting center of testmass.**

2. Step roll off above 1kHz

**Candidate: (non) rigidity of the testmass**