

# Large Interferometers for small displacements:



A technological view of  
Gravitational Wave detection



**Stefan Hild, University of Glasgow**

OFS-20, Edinburgh, October 2009

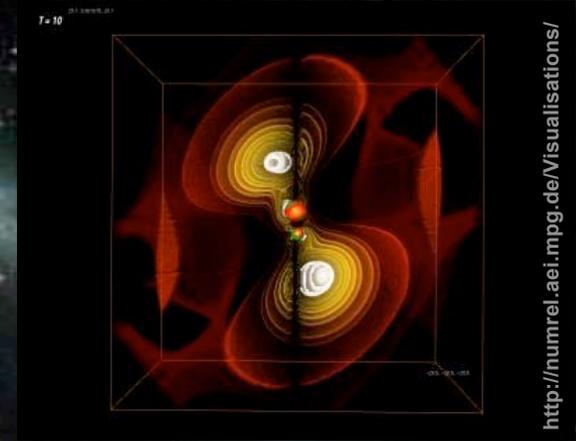
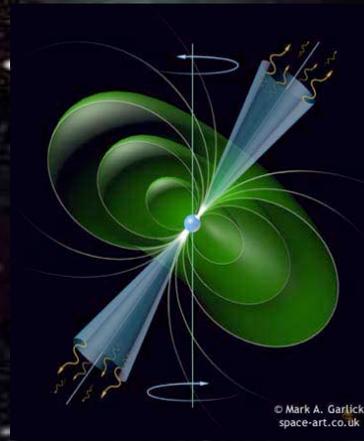
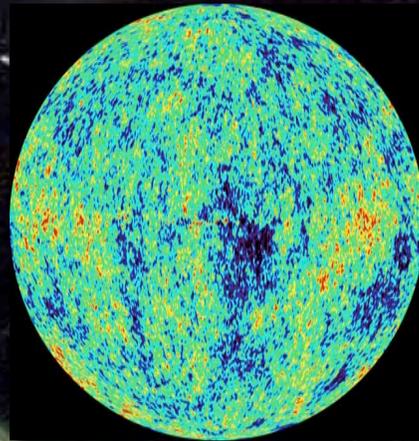
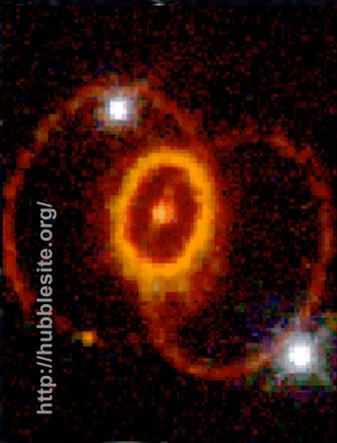


# Outline

- ➔ Overview of Gravitational Wave detection
- ➔ Optical technology for high precision interferometry
  - Simple Michelson interferometer
  - Power Recycling
  - Arm cavities
  - Signal Recycling
  - Standard Quantum limit
- ➔ Examples of new technologies for future Gravitational wave detectors
  - High power laser, Laguerre Gauss modes, Quantum-non-demolition

# The most violent events in Universe are in our reach !

<http://hubblesite.org/>

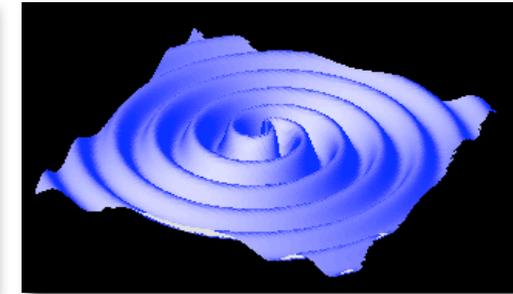
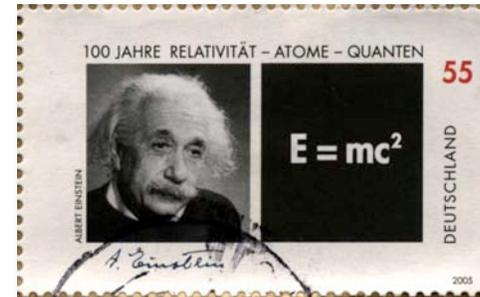


Soon we will be able to listen to Supernovae, colliding black holes and even the aftermath of the Big Bang using Gravitational waves.

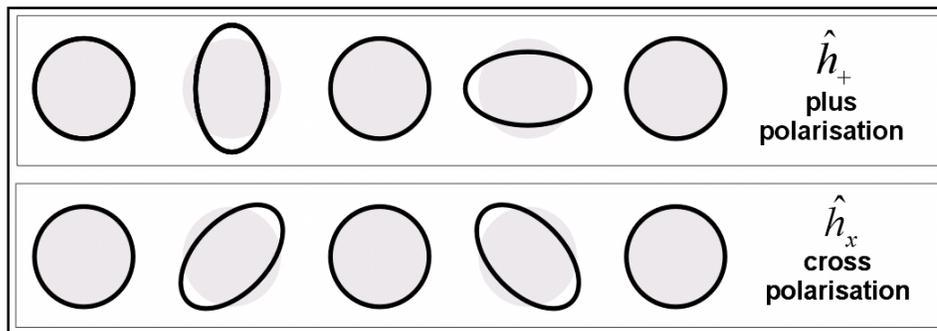


# Gravitational Waves: Ripples in space time

- ➔ GW are consequence of General Relativity.
- ➔ GW are caused by asymmetric accelerated masses.
- ➔ GW change the metric of space time.
- ➔ Quadrupole waves.



- ➔ **We know that GW exist:**  
Indirect detection by Taylor and Hulse (1993 Nobel Prize).
- ➔ **No direct detection so far.**  
On going search with kilometer-long Michelson interfero-meters looking for tiny length changes.





# Why haven't we measured GW so far?

Stress Energy Tensor

Metric Tensor

$$\overline{\overline{T}} = \frac{c^4}{8\pi G} \overline{\overline{G}}$$

Analogon: Hooke's law

$$(\vec{F} = k\vec{x})$$

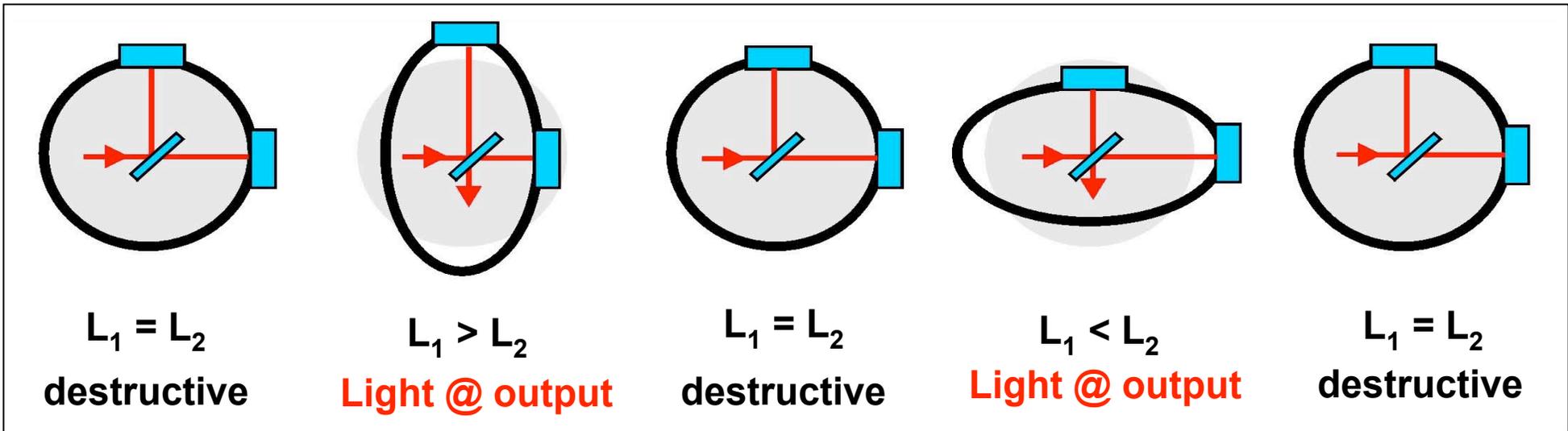
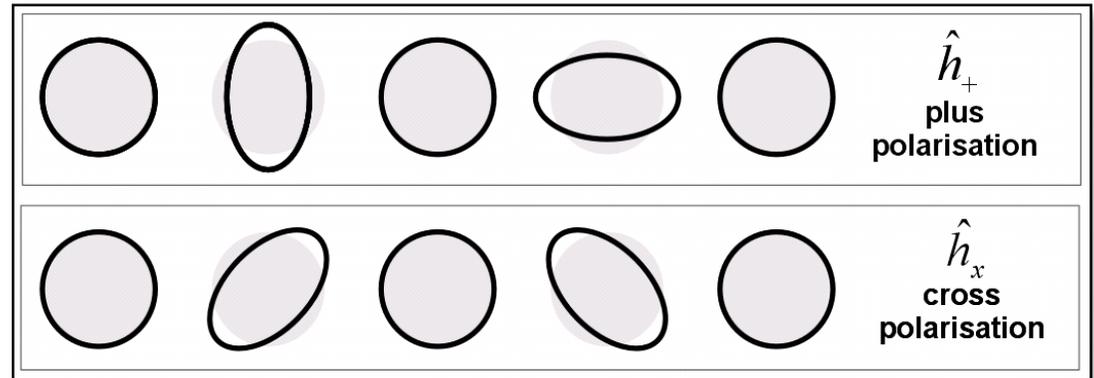
Stiffness of space time

$$\frac{c^4}{8\pi G} \approx 5 \cdot 10^{42}$$

- ➔ Space time is extremely stiff !
- ➔ Length changes caused by GW are really tiny ( $<10^{-21}$ ) !

# How can we detect gravitational waves?

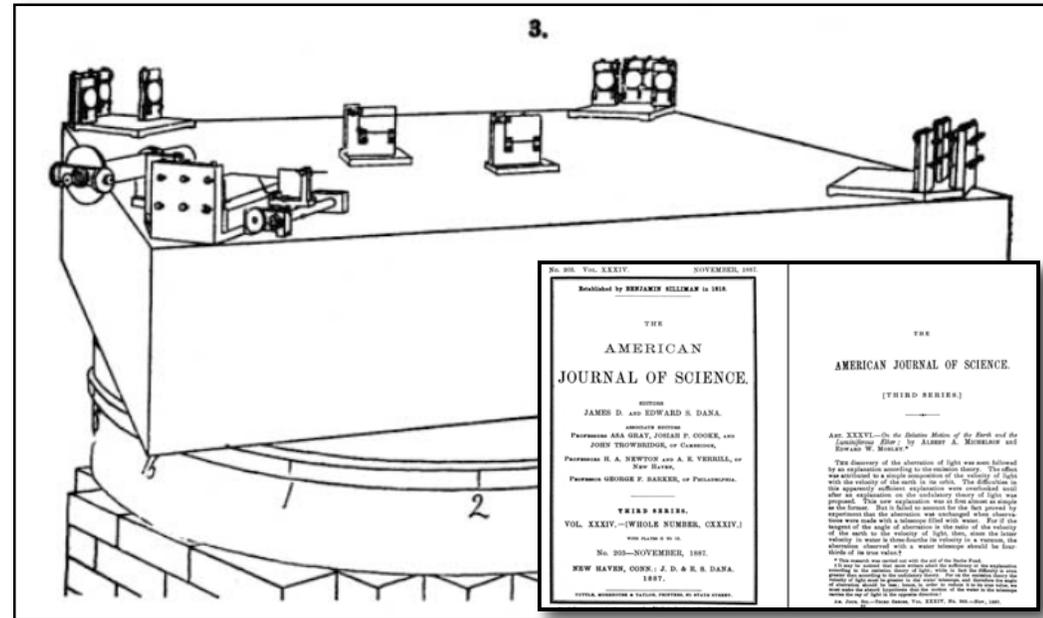
A Michelson interferometer is the ideal instrument to measure relative length changes.



# We have come a long way ...



- ➔ The first Michelson interferometer: Experiment performed by Albert Michelson in Potsdam 1881.
- ➔ Measurement accuracy 0.02 fringe



- ➔ Michelson and Morley 1887 in Cleveland.

**ART. XXXVI.—On the Relative Motion of the Earth and the Luminiferous Ether; by ALBERT A. MICHELSON and EDWARD W. MORLEY.\***



# State-of-the-art Michelson Interferometer





# State-of-the-art Michelson Interferometer



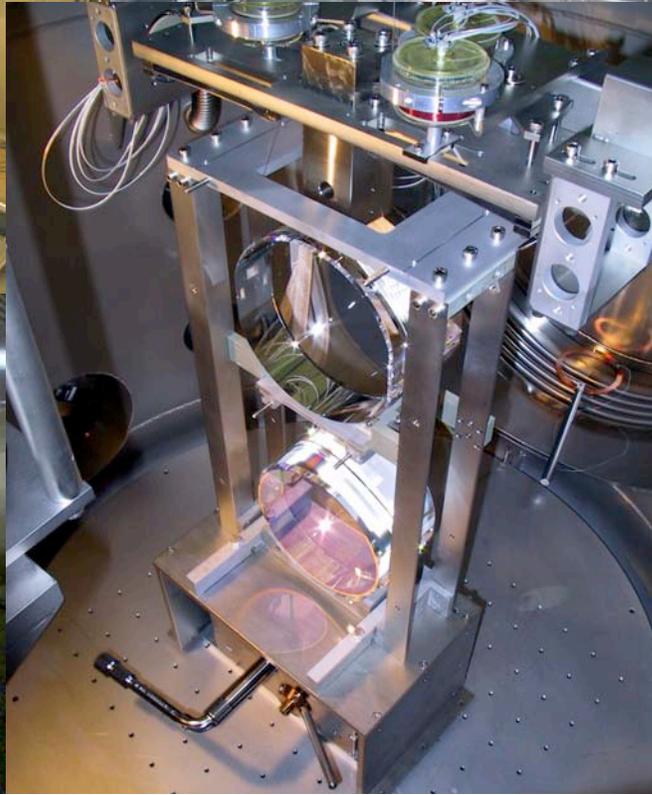


# State-of-the-art Michelson Interferometer



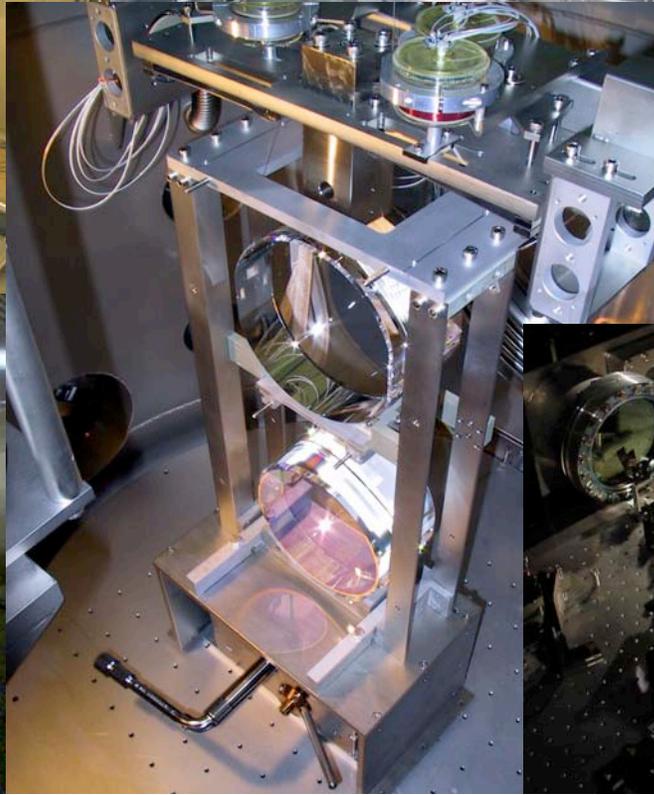
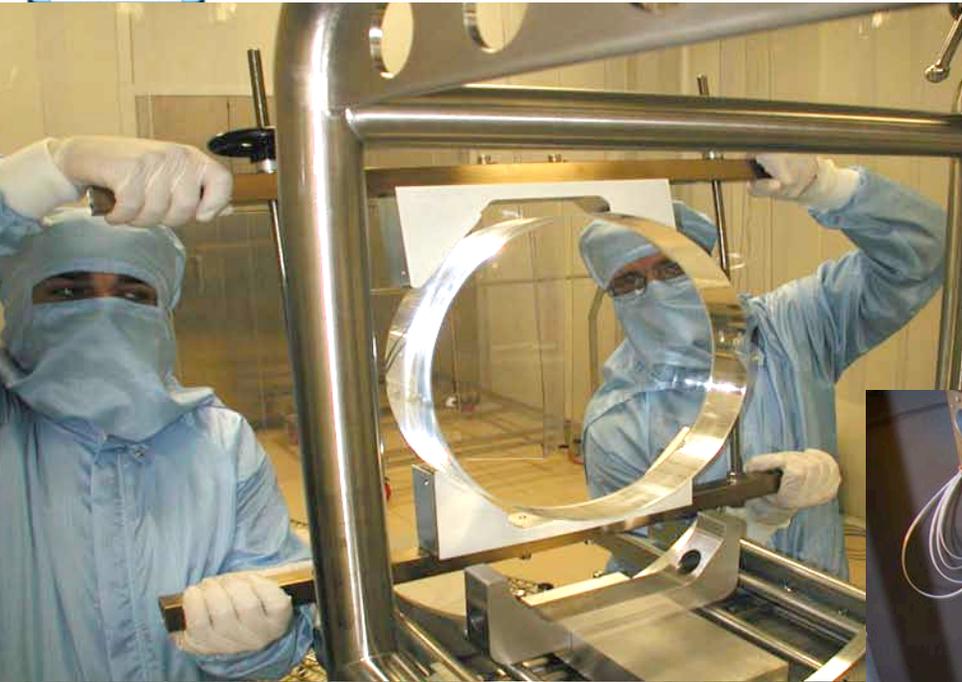


# State-of-the-art Michelson Interferometer



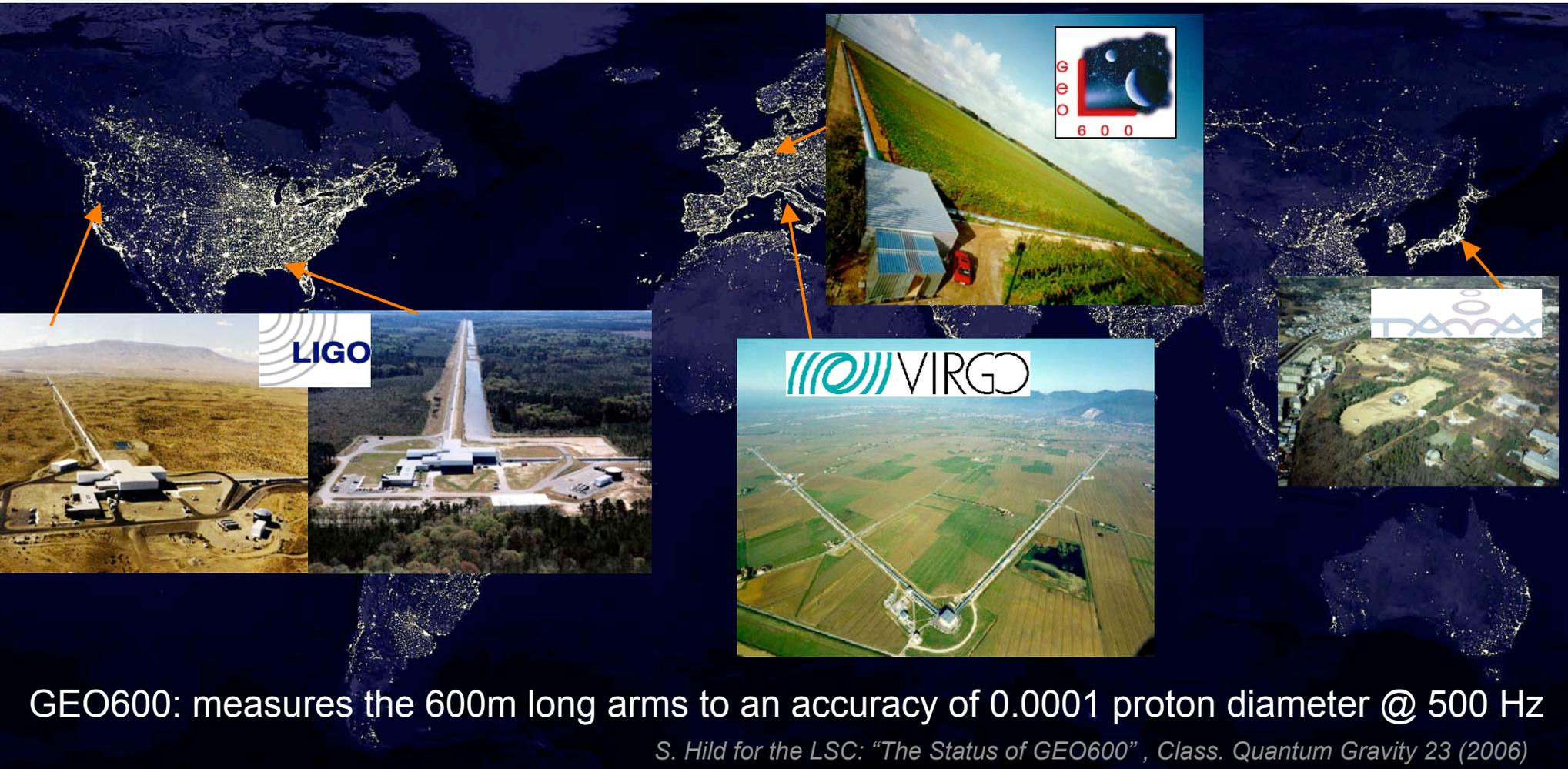


# State-of-the-art Michelson Interferometer





# Today's network of GW detectors



GEO600: measures the 600m long arms to an accuracy of 0.0001 proton diameter @ 500 Hz

*S. Hild for the LSC: "The Status of GEO600", Class. Quantum Gravity 23 (2006)*



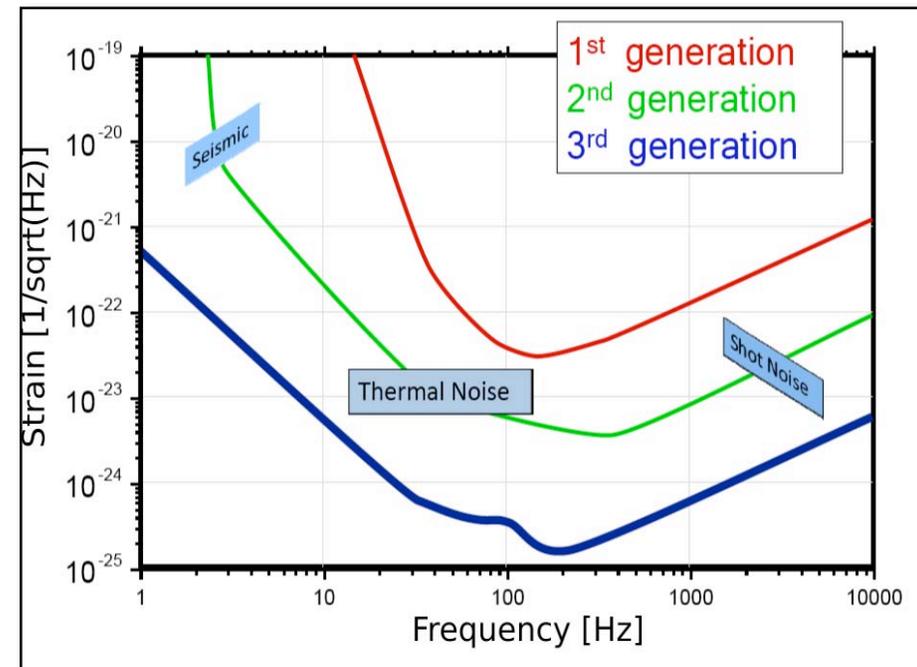
# Status and future of GW observatories

- ➔ **1st** generation successfully completed:
  - Long duration observations ( $\sim 1$ yr) in coincidence mode of 5 observatories.
  - Spin-down upper limit of the Crab-Pulsar beaten!
- ➔ **2nd** generation on the way:
  - End of design phase, construction about to start (or even started)
  - **10 times better sensitivity** than 1st generation.  $\Rightarrow$  Scanning **1000** times larger volume of the Universe
- ➔ **3rd** generation at the horizon:
  - FP7 funded design study
  - **100 times better sensitivity** than 1st generation.  $\Rightarrow$  Scanning **1000000** times larger volume of the Universe

1G = GEO600 / LIGO / Virgo

2G = Advanced LIGO, GEO-HF, A-Virgo

3G = Einstein Telescope





# Outline

## ➔ Overview of Gravitational Wave detection

## ➔ Optical technology for high precision interferometry

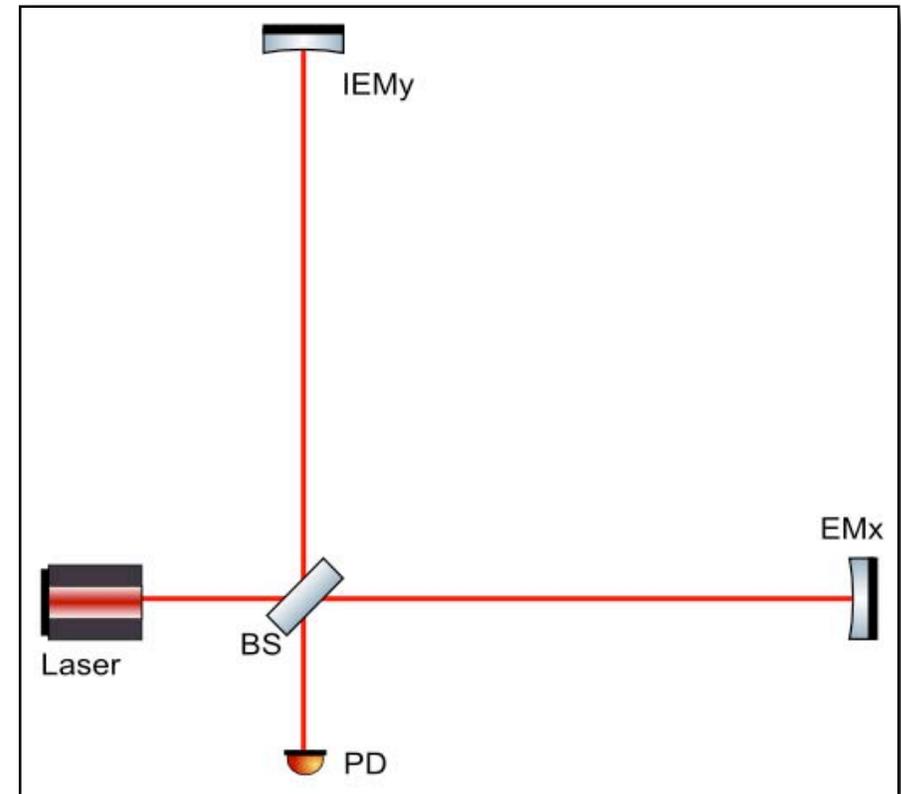
- Simple Michelson interferometer
- Power Recycling
- Arm cavities
- Signal Recycling
- Standard Quantum limit

## ➔ Examples of new technologies for future Gravitational wave detectors

- High power laser, Laguerre Gauss modes, Quantum-non-demolition

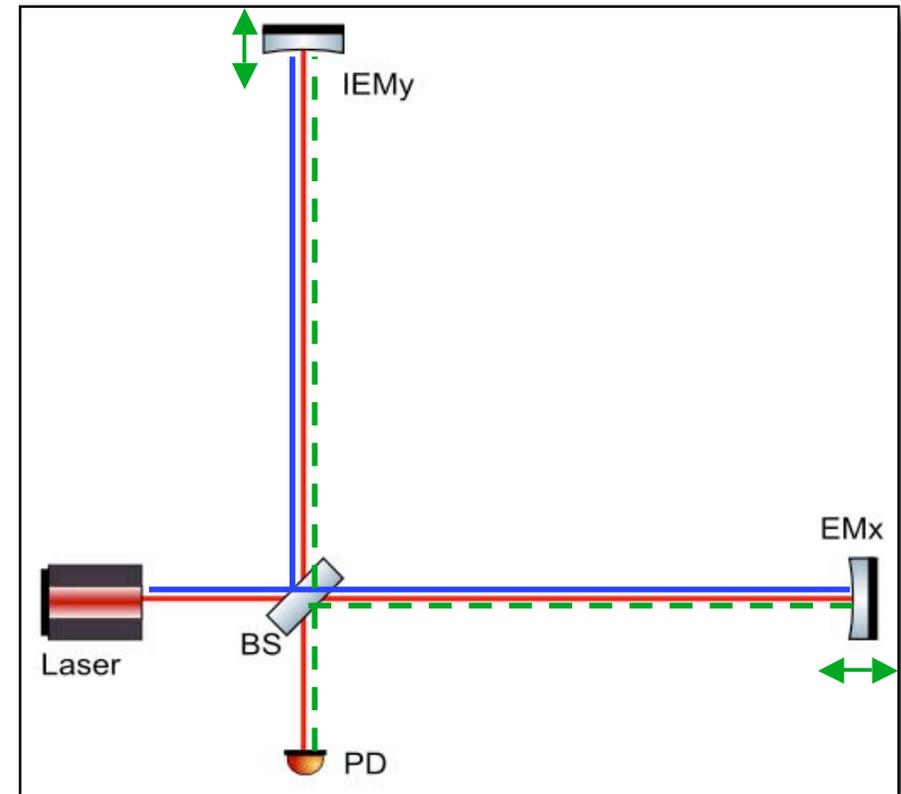
# Interferometry: A simple Michelson

- ➔ How does a simple Michelson interferometer work?
- ➔ Aim: Measure lengths difference of the two perpendicular arms.
- ➔ Light from laser:
  - is split by beamsplitter,
  - travels along the arms,
  - bounces off the end mirrors
  - travels back beamsplitter
- ➔ Measurement is done by comparing the phase of the two returning beams.



# Interferometry: A simple Michelson

- ➔ Differential arm lengths changes can be described by the creation of phase modulation sidebands.
- ➔ Operation point = Dark fringe
  - Carrier light leaves the IFO towards the laser
  - Signal sidebands leaves towards the photodiode
- ➔ Many technical noises (frequency noise, laser amplitude noise) suppressed by common mode rejection.
- ➔ Null-measurement !!

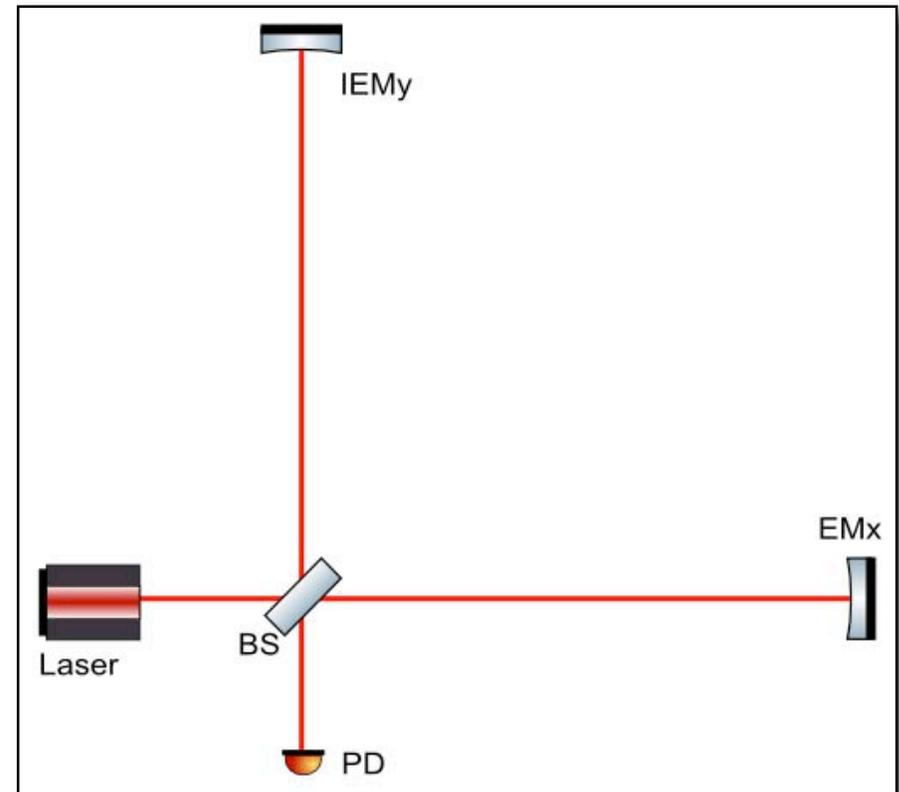


# Interferometry: A simple Michelson

- ➔ Who can we improve our sensitivity to gravitational waves?
- ➔ GW signal scales with storage time of the light in the arms:
  - Increasing arm length
  - Make use of recycling techniques
- ➔ Major noise source limiting our sensitivity is shot noise.
  - Shot noise prop.  $\sqrt{\text{power}}$
  - GW signal scales linear with power

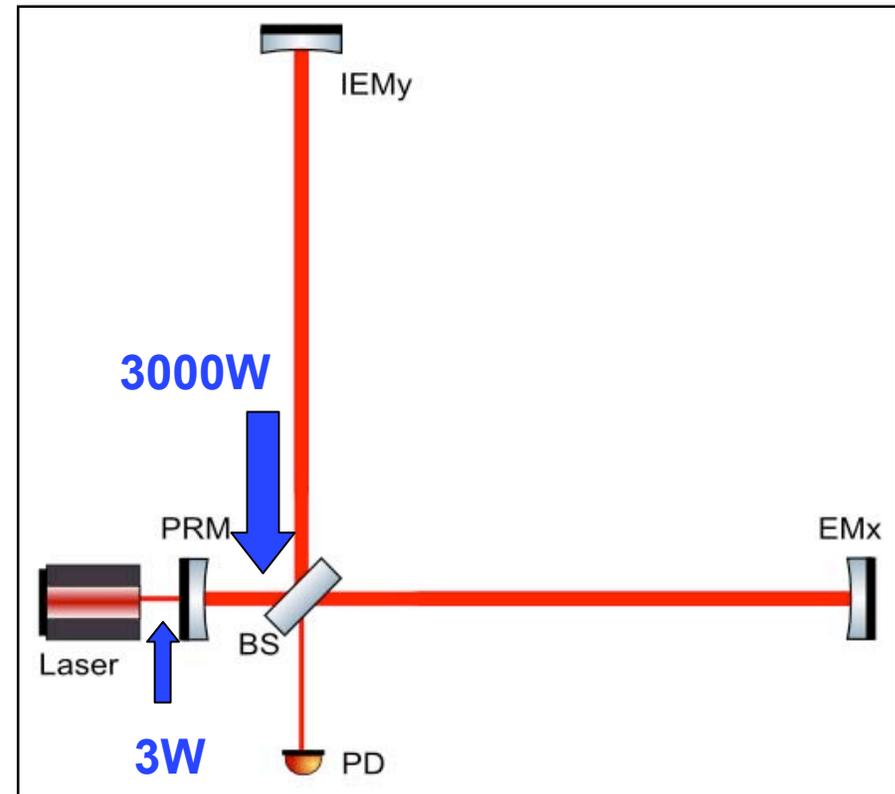
## Our Goal:

- Increase storage time in the arms
- Increase circulating light power



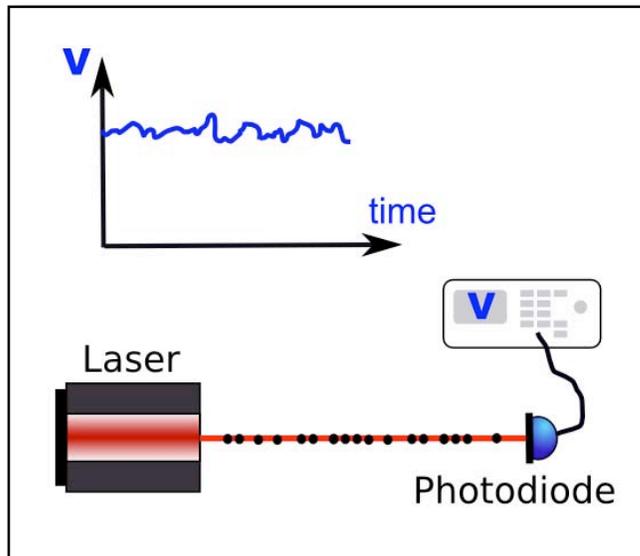
# Interferometry: Power Recycling

- ➔ If operated on the dark fringe the Michelson looks from the laser like a mirror.
- ➔ Instead of 'wasting' light we insert a semi-transparent power-recycling mirror (PRM) to send the light back to the interferometer.
- ➔ In GEO600 a power recycling factor of 1000 is realised.

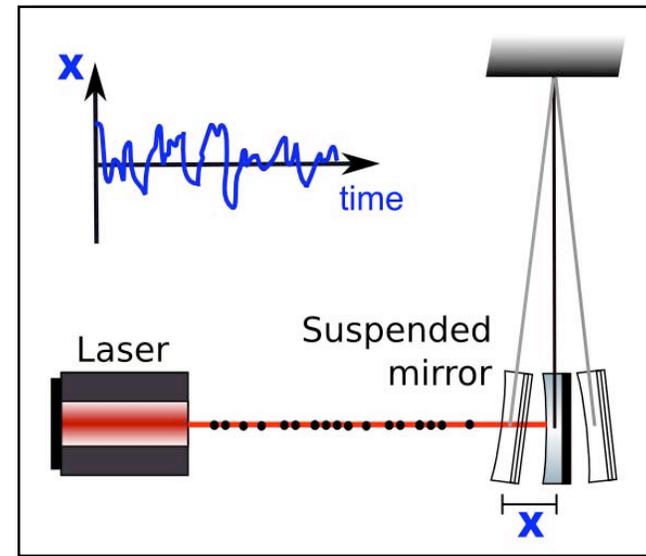


# Quantum noise components

- ➔ Quantum noise is comprised of **photon shot noise** at high frequencies and **photon radiation pressure noise** at low frequencies.
- ➔ The photons in a laser beam are not equally distributed, but follow a Poisson statistic.



**photon shot noise**



**photon radiation pressure noise**

# The Standard Quantum Limit (SQL)

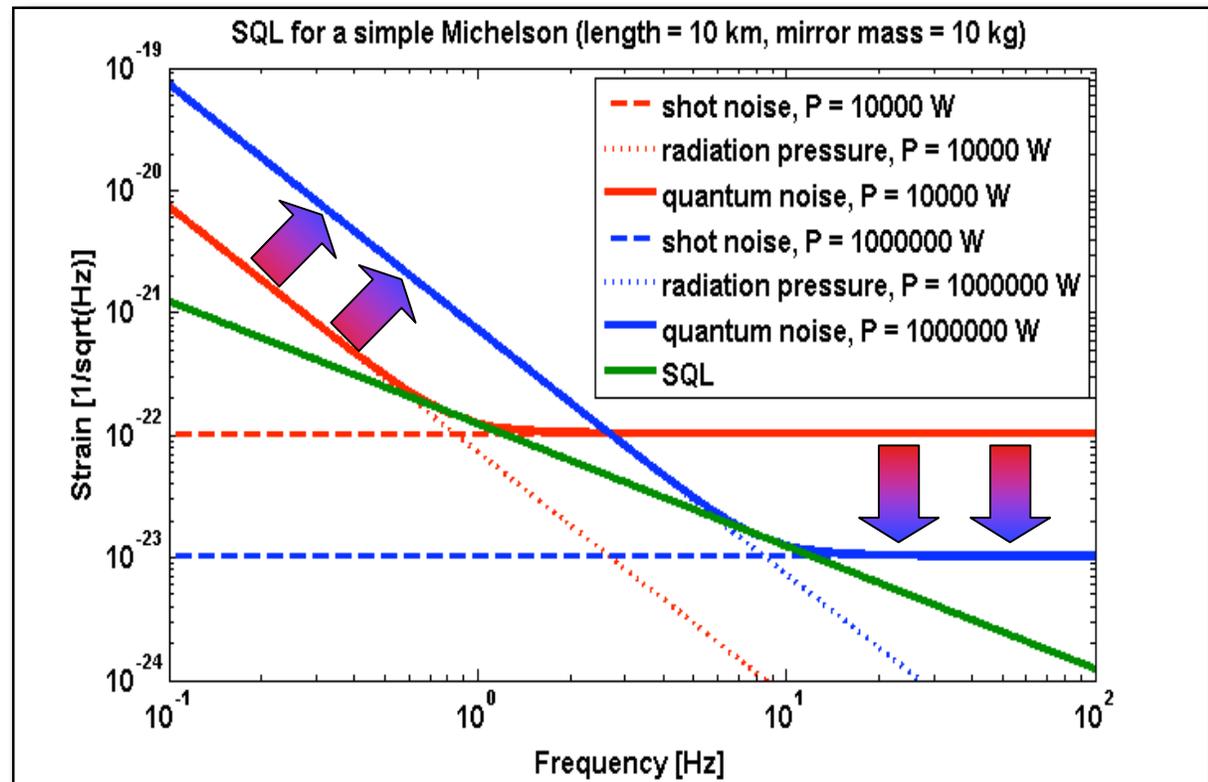
- While shot noise contribution decreases with optical power, radiation pressure level increases:

$$h_{\text{sn}}(f) = \frac{1}{L} \sqrt{\frac{\hbar c \lambda}{2\pi P}}$$

wavelength  
optical power

$$h_{\text{rp}}(f) = \frac{1}{m f^2 L} \sqrt{\frac{\hbar P}{2\pi^3 c \lambda}}$$

Mirror mass  
Arm length

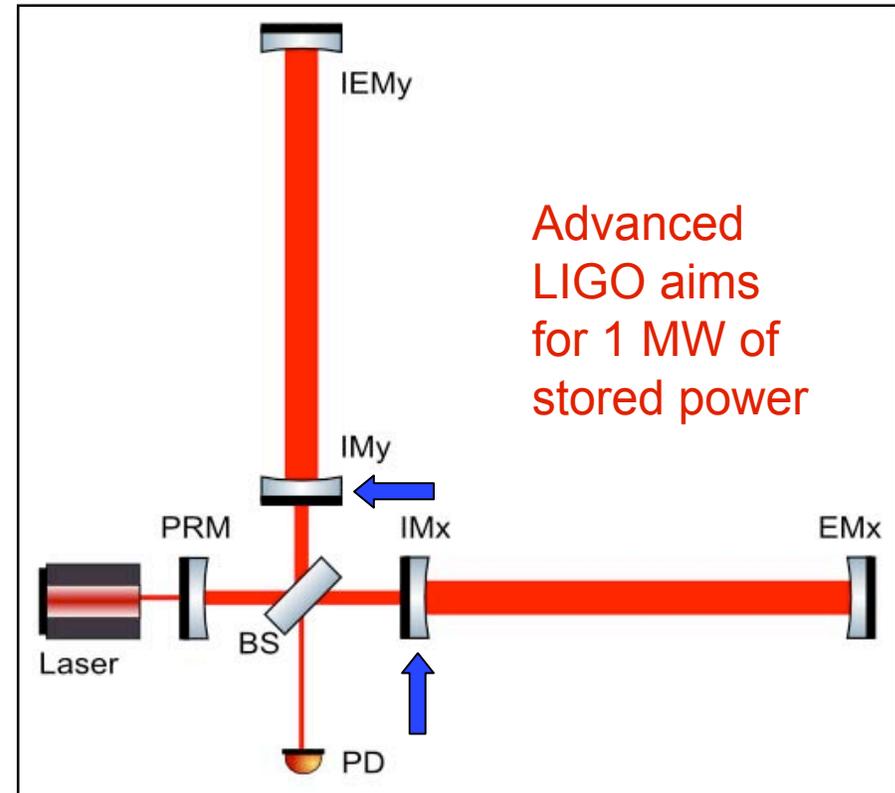
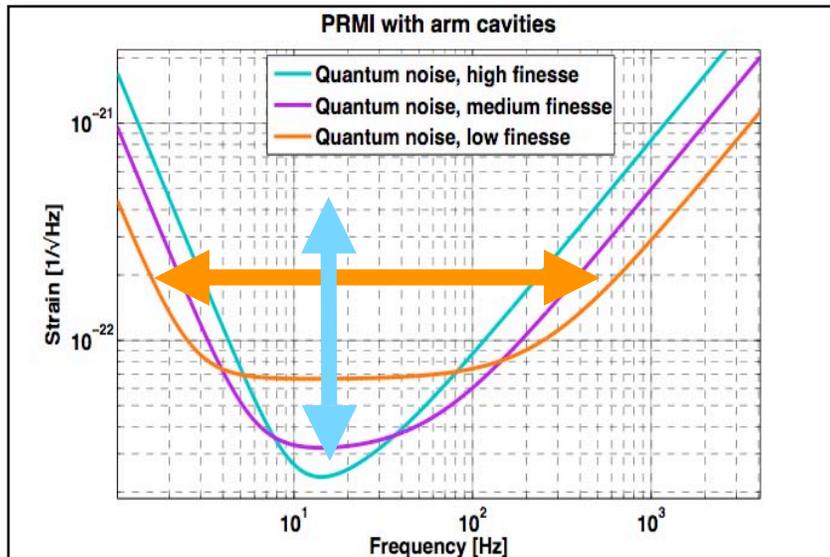


- The SQL is the minimal sum of shot noise and radiation pressure noise.
- Using a classical quantum measurement the SQL represents the lowest achievable noise.

*V.B. Braginsky and F.Y. Khalili: Rev. Mod. Phys. 68 (1996)*

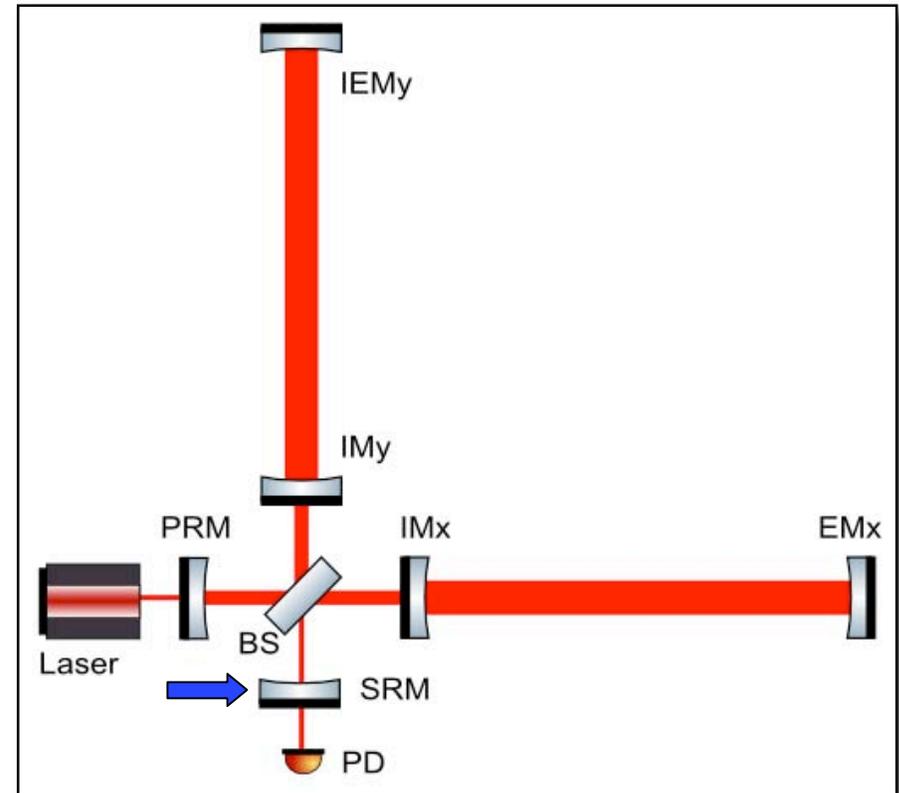
# Interferometry: Arm cavities

- ➔ Increasing the storage time in the arms by using arm cavities.
- ➔ Finesse of the arm cavities determines bandwidth of GW detector.

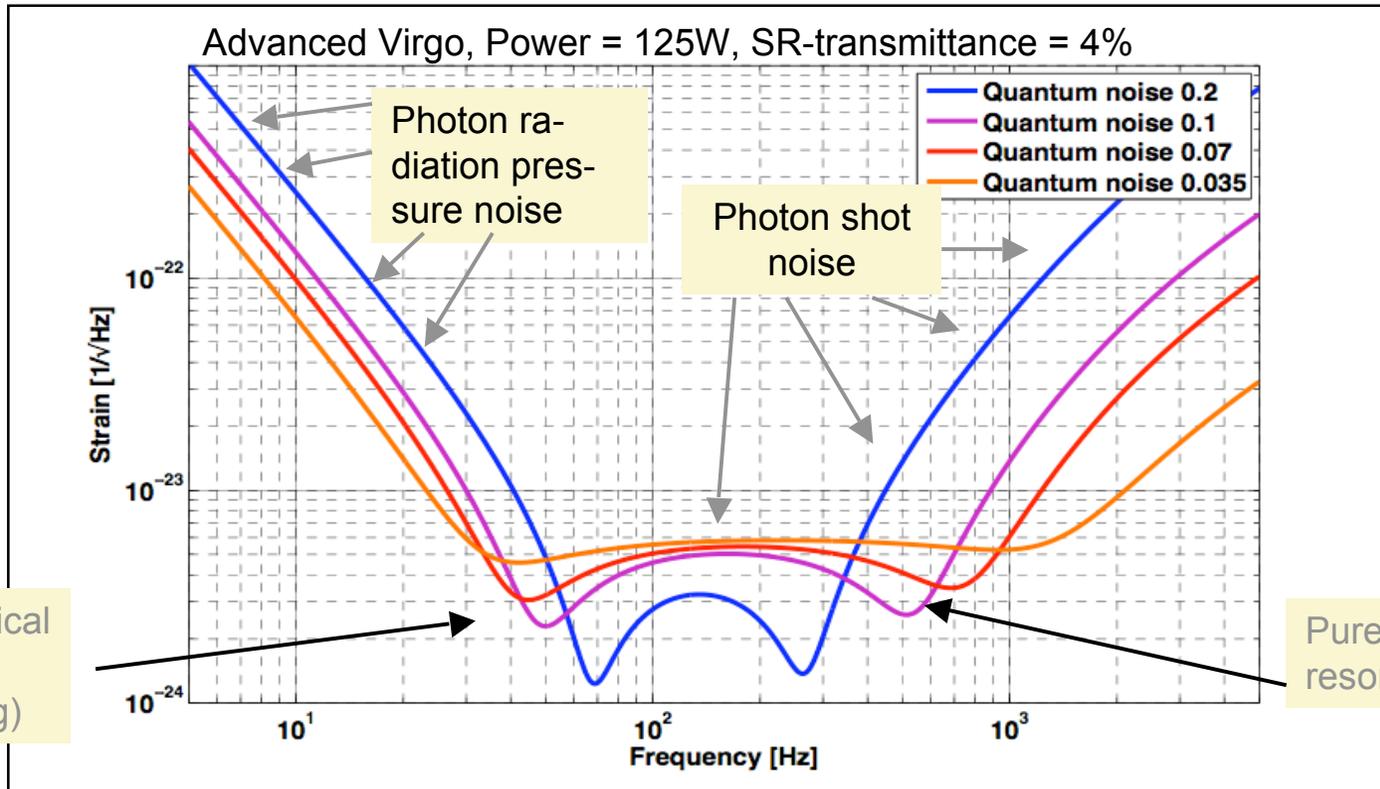


# Interferometry: Signal Recycling

- ➔ Inserting a semi-transparent signal recycling mirror (SRM) at the output of the Michelson.
  - Increasing the signal storage time
- ➔ Signal Recycling allows to shape Quantum noise via two knobs:
  - Bandwidth
  - Frequency of maximal sensitivity
- ➔ Very handy for adjusting the detector sensitivity to astrophysical targets of interest.



# Signal-Recycling (de)tuning



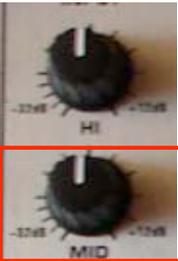
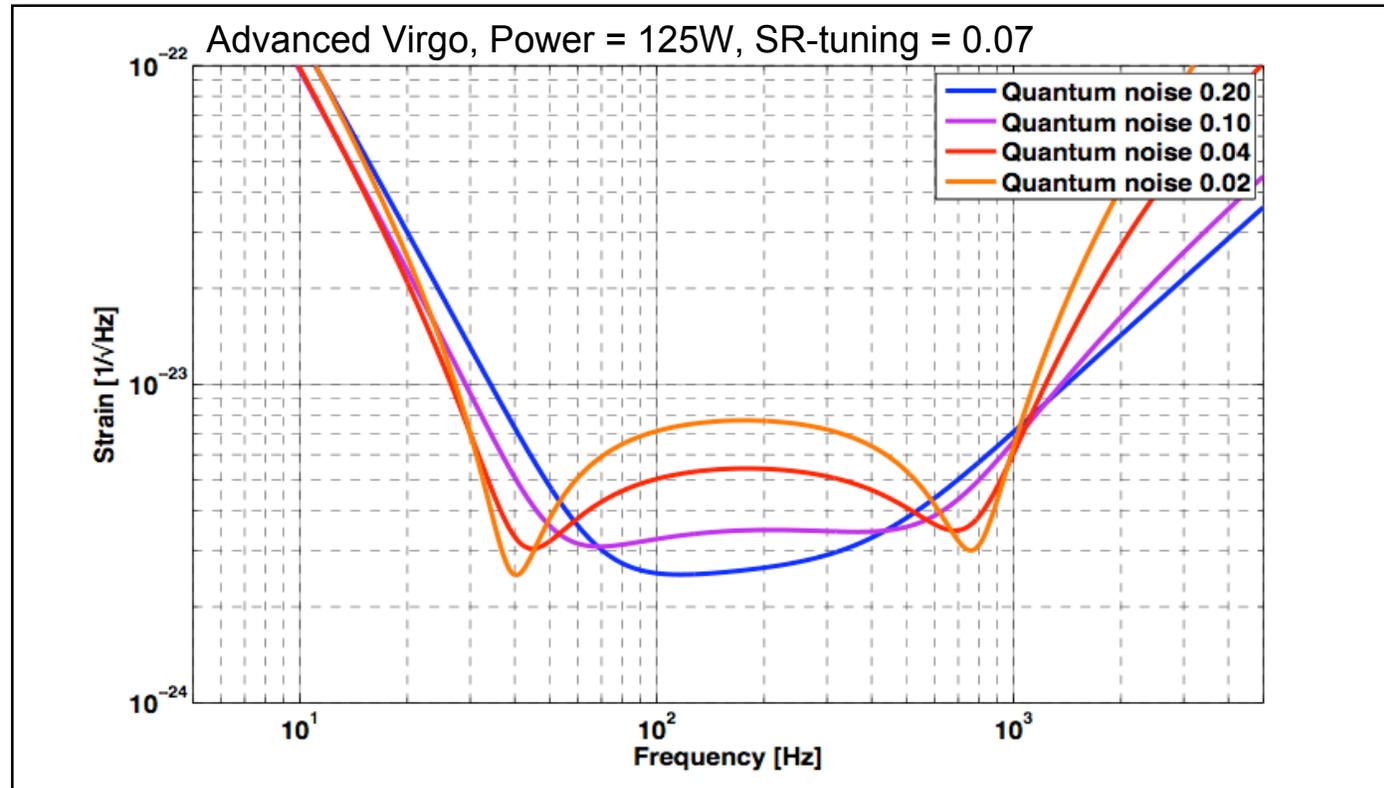
knob 1

Opto-mechanical Resonance (Optical spring)

Pure optical resonance

- Modifying the Signal recycling detuning frequency by changing the position of the signal recycling mirror by a few nanometers.

# Signal-Recycling mirror transmittance



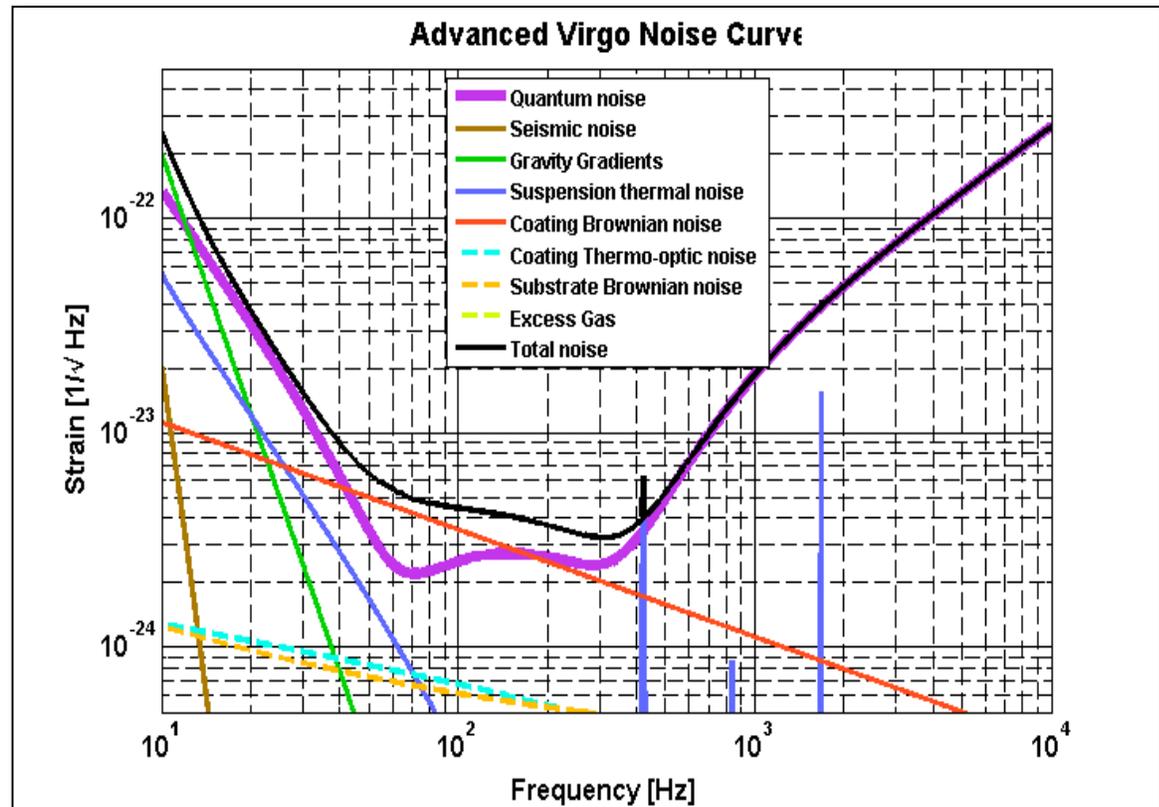
knob 2

- ➔ Modifying the Signal recycling bandwidth by changing the reflectance of the signal recycling mirror by a few nanometers.



# Fundamental noise limits for future GW detectors

- ➔ Future GW detectors (such as Advanced LIGO or Advanced Virgo) will be limited by **quantum noise** at nearly all frequencies of interest.
- ➔ The second major noise source is **Brownian noise** of the **dielectric coating** layers.
- ➔ Other noises that need to be treated with care:
  - Gravity gradient noise
  - Seismic noise
  - Suspension thermal noise



*S. Hild et al: "Sensitivities curves for the Advanced Virgo Preliminary Design", Virgo note VIR-101A-08, available at <https://pub3.ego-gw.it/codifier/index.php>*

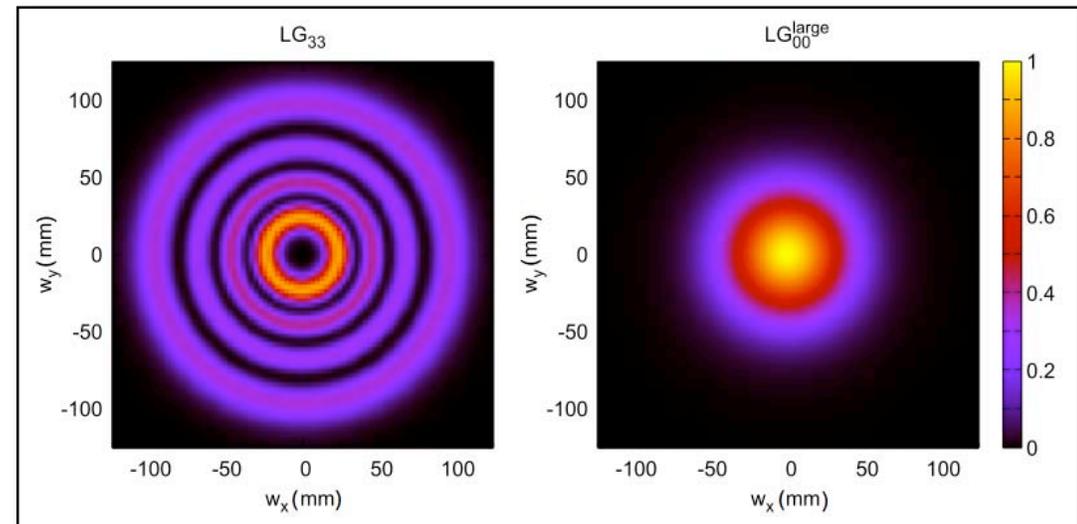


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# Laguerre Gauss modes to reduce thermal noise

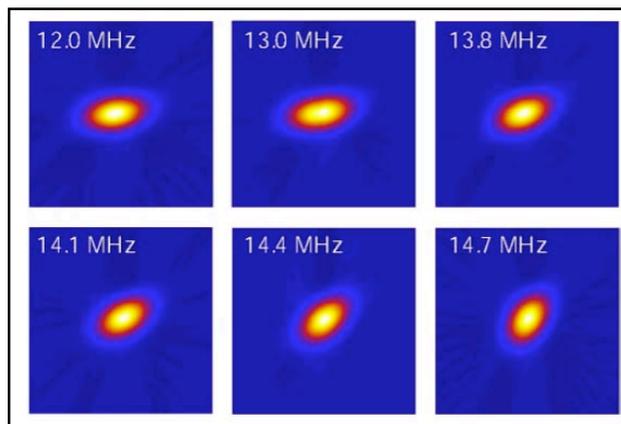
- ➔ Mirror thermal noise can be reduced by a factor of a few by using higher order LG modes instead of  $TEM_{00}$
- ➔ By distributing the power more homogeneously over the mirror surface one can average better over the local thermal fluctuations
- ➔ We showed that interferometry (creation of errorsignal, misalignment effects etc) are similar for  $TEM_{00}$  and  $LG_{33}$ .



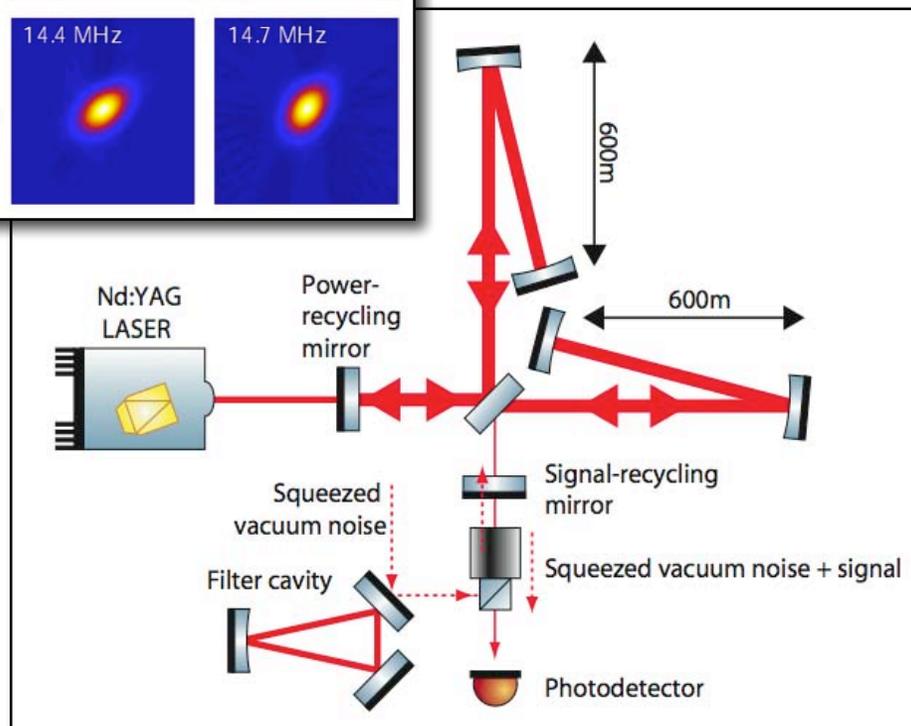
Chelkowski, Hild, Freise: PRD 79, 122002

# Injection of Squeezed Light

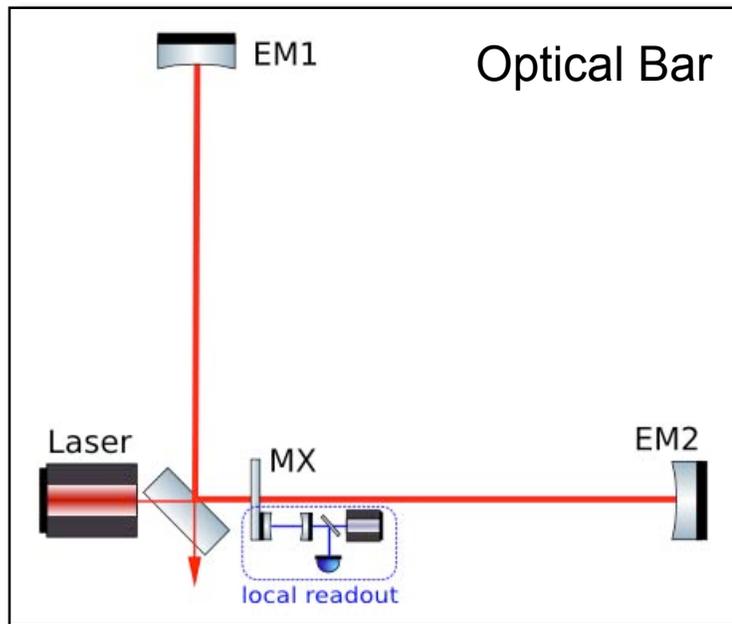
- ➔ Injection of squeezed light will reduce photon shot noise / quantum noise.
- ➔ Squeezed light sources available now:
  - **10dB** squeezing
  - Frequencies as low as **10Hz**
- ➔ Implementation of squeezing in GEO600 happening right now.
- ➔ First time demonstration in a big interferometer.



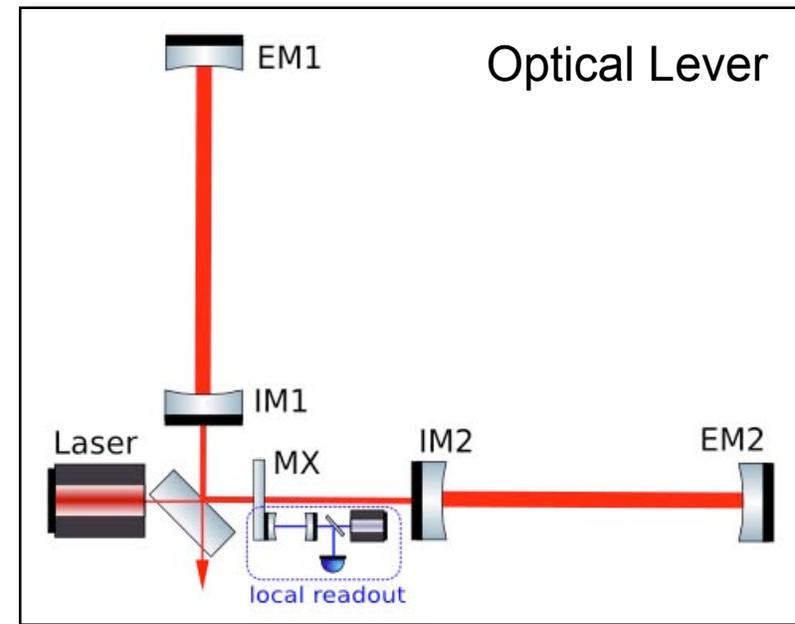
Chelkowski et al:  
PRA 71, 013806



# Quantum-Non-Demolition Techniques



V.B. Braginsky and F.Y. Khalili: "Nonlinear meter for the gravitational wave antenna", *Phys. Lett. A* 218 (1996).



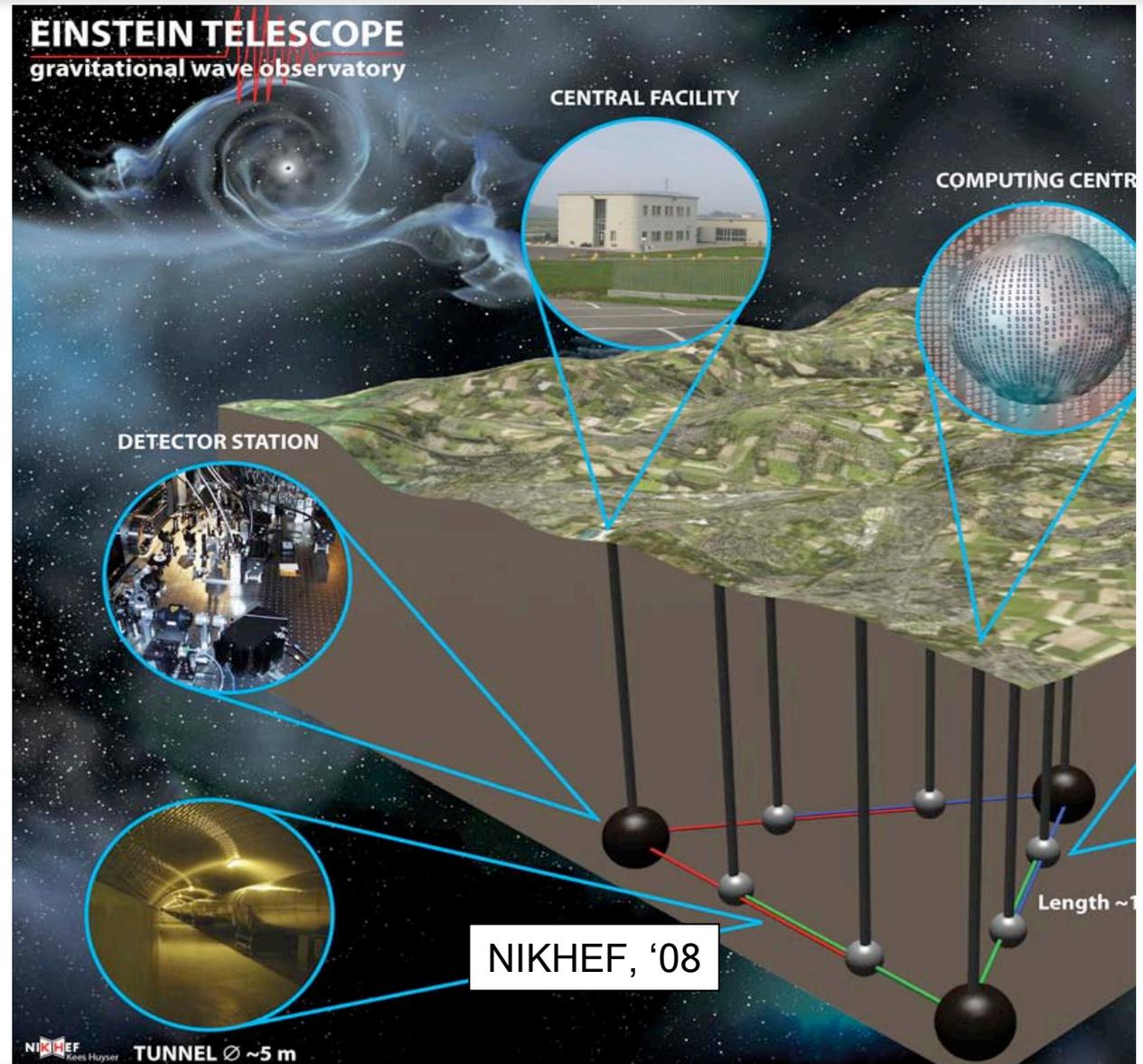
F.Y. Khalili: "The 'optical lever' intracavity readout scheme for gravitational-wave antennae", *Phys. Lett. A* 298 (2002).

- Very light mirror (MX) is coupled to the movement of EM1 and EM2 via optical springs.
- MX can then locally read out by a small **local meter** without disturbing the quantum states in the main instrument (QND measurement).
- Optical lever: introducing arm cavities increases the movement of MX by the Finesse of the arm cavity.



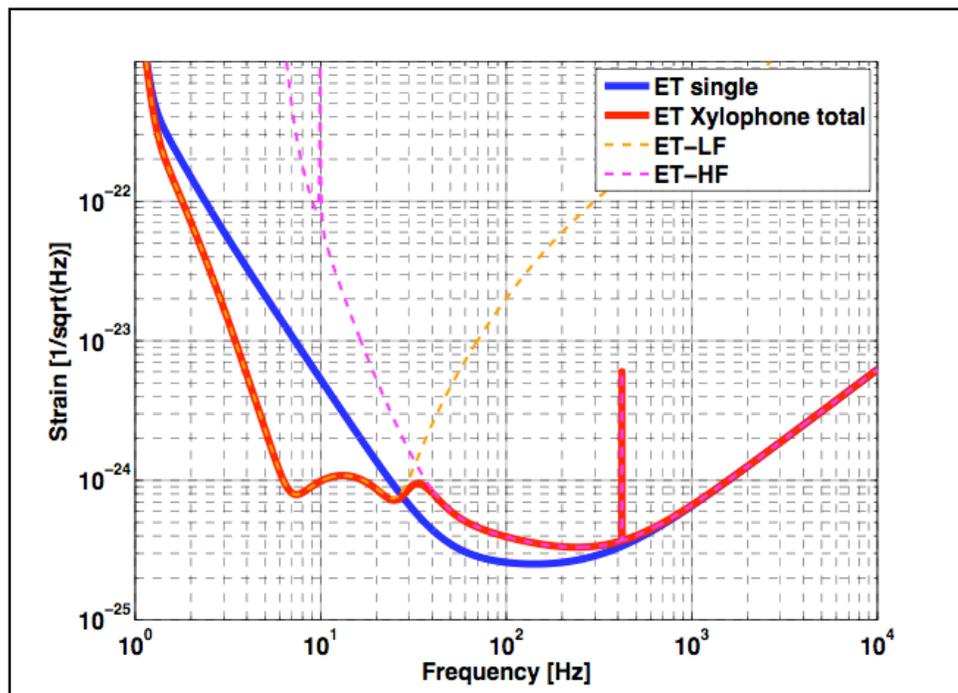
# Einstein Telescope

- ➔ Start around 2020(?)
- ➔ Underground location
- ➔ ~30km integrated tunnel length (?)
- ➔ Triangular shape
- ➔ **Myriads of new possibilities and challenges !!**
- ➔ **Plenty of new Science...**





# Xylophone: More than one detector to cover the full bandwidth



S.Hild et al : arXiv:0906.2655

Parameter	ET-HF	ET-LF
Arm length	10 km	10 km
Mirror material	Fused Silica	Silicon
Mirror diameter / thickness	62 cm / 30 cm	62 cm / 30 cm
Mirror masses	200 kg	211 kg
Laser wavelength	1064 nm	1550 nm
Input power (after IMC)	500 W	3 W
Arm power	3 MW	18 kW
SR-phase	tuned (0.0)	detuned (0.6)
SR transmittance	10 %	20 %
Quantum noise suppression	10 dB	10 dB
Beam radius	12 cm	12 cm
Beam shape	LG <sub>33</sub>	TEM <sub>00</sub>
Temperature	290 K	10 K
Suspension	Superattenuator	5 × 10 m
Seismic (for $f > 1$ Hz)	$1 \cdot 10^{-7} \text{ m}/f^2$	$5 \cdot 10^{-9} \text{ m}/f^2$
Gravity gradient subtraction	none	factor 50

**Low Frequency IFO:** low optical power, cryogenic test masses, sophisticated low frequency suspension, underground, heavy silicon test masses, laser at 1550nm.

**High Frequency IFO:** high optical power, room temperature, surface location, squeezed light



# Summary

- ➔ Hunting gravitational waves requires plenty innovative optical technology.
- ➔ Pushing optics and interferometry towards their limits (and sometimes even beyond!) we set up an international network of extremely sensitive, km-long Michelson interferometers.
- ➔ There is an exciting future waiting for us. Many new optical technologies need to be developed, adapted, prototyped and implemented.



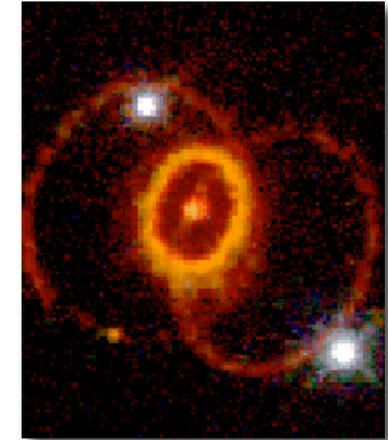
**Thanks very much for  
your attention!**

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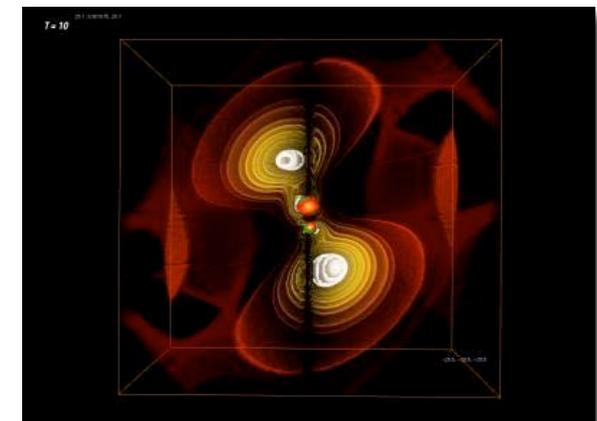


# Gravitational waves: A new way of exploring the Universe

- ➔ Nearly all of our current knowledge of the cosmos is based on observation of electromagnetic radiation (visible light, radio astronomy, infrared, ...).
- ➔ Gravitational astronomy can provide completely new insight to the universe:
  - Multimessenger observations: We can learn more about things we already see in the electromagnetic spectrum by also seeing their GW emission (for instance supernovae).
  - Exclusive GW observations: There are objects that can only be seen by their GW emission



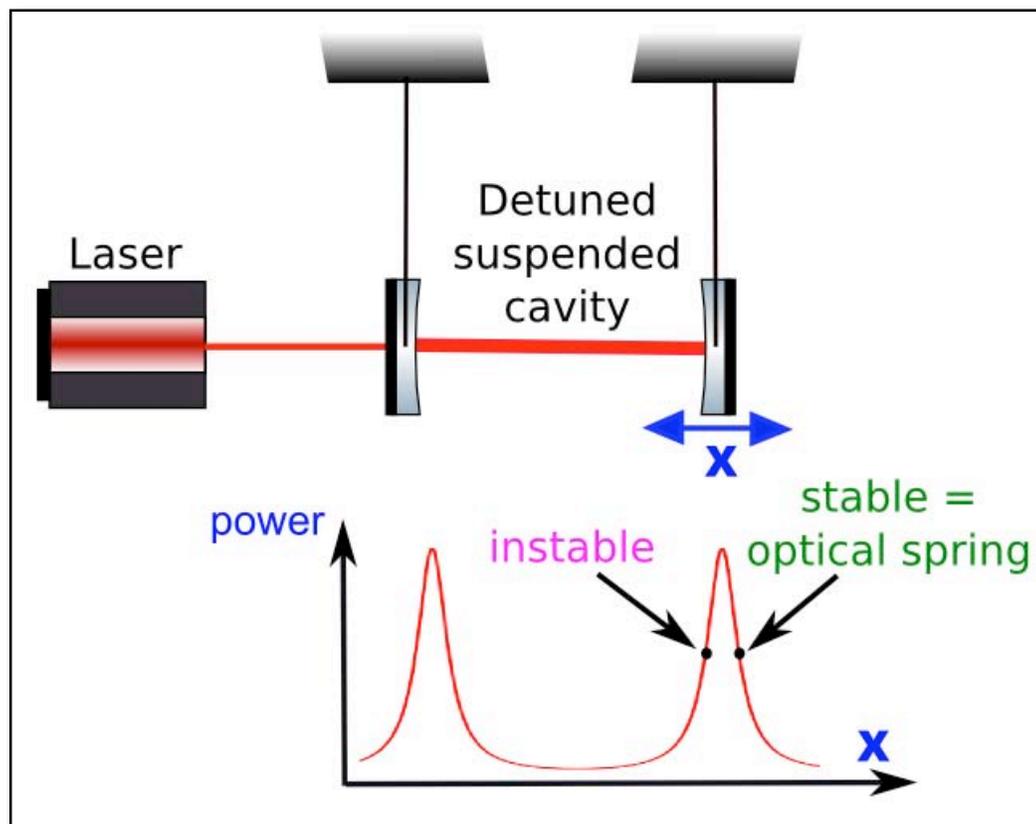
<http://hubblesite.org/>



<http://numrel.aei.mpg.de/Visualisations/>

# Optical Springs & Optical Rigidity

- ➔ Detuned cavities can be used to create optical springs.
- ➔ Optical springs couple the mirrors of a cavity with a spring constant equivalent to the stiffness of diamond.
- ➔ In a full Michelson interferometer detuned Signal Recycling causes an optical spring resonance.





# High power lasers at 1064nm

- ➔ Advanced Ligo will feature a 200W laser.
  - Low power: NPRO
  - Medium power: amplifier
  - High power: Slave laser
- ➔ Prestabilized in frequency and power
- ➔ Achieved RIN of about  $3e-9$ .

