Near-Maximal Two-Photon Entanglement for Optical Quantum Communication at 2.1 μm

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(Received 18 June 2021; revised 9 September 2021; accepted 27 October 2021; published 30 November 2021)

Owing to a reduced solar background and low propagation losses in the atmosphere, the 2- to 2.5-μm waveband is a promising candidate for daylight quantum communication. This spectral region also offers low losses and low dispersion in hollow-core fibers and in silicon waveguides. We demonstrate near-maximally entangled photon pairs at 2.1 μm that could support device-independent quantum key distribution (DIQKD), assuming sufficiently high channel efficiencies. The state corresponds to a positive secure-key rate (0.254 bits/pair, with a quantum bit error rate of 3.8%) based on measurements in a laboratory setting with minimal channel loss and transmission distance. This is promising for the future implementation of DIQKD at 2.1 μm.

DOI: 10.1103/PhysRevApplied.16.L051005

Introduction.—Entanglement remains a key ingredient for many emerging quantum technologies based on communication and information processing protocols such as quantum key distribution (QKD) [1–3], superdense coding [4], and state teleportation [5]. The workhorses for the implementation of these protocols until now have been light sources at visible and telecom wavelengths based on both guided-wave and free-space transmission [6]. In recent years, satellite-to-ground links have emerged as the most promising option for long-distance QKD [7–12]. A critical challenge for satellite-to-ground QKD is the limited operability in daylight due to excess background in the telecom and visible bands [13]. As a result, most demonstrations to date rely on nighttime operation, with only a few exceptions [14]. Moreover, entanglement-based or device-independent (DI) approaches in daylight are still to be demonstrated. DI implementations here refer to those in which no assumptions are made about the way the QKD devices work or on what quantum system they are based [15,16]. In addition, the push towards satellite-based communication networks is leading to a paradigm shift in QKD towards DI implementations that must support both fibre and free-space optical links.

The 2- to 2.5-μm spectral region is rapidly becoming a highly promising optical telecommunications band with significant advantages over the traditional telecom C-band (1550 nm), making it crucial to develop and investigate quantum sources and measurement capabilities in this waveband. For example, the 2-μm band has been demonstrated to have minimal losses in the hollow-core photonic band gap fiber (HCF) [17], which is an emerging transmission-fiber alternative due to its ultralow nonlinearity, and providing the lowest available latency. Losses of 2.5 dB/km in the 2-μm region have been demonstrated using HCFs [18], with scope for further reduction potentially beyond the minimum attenuation of 0.14 dB/Km in pure-silica-core fiber [19], which is determined by fundamental scattering and absorption processes. Indeed, using the nested antiresonant nodeless fiber (NANF) design, a record-low loss of 0.28 dB/km has recently been demonstrated in the telecom C-band and L-band [20]. However, NANFs have yet to be studied in the 2-μm region.

In addition, although the 2-μm band enjoys similar atmospheric transparency as the telecom C-band, the solar background is up to 3 times lower [21], making it especially promising for free-space optical communications during daytime. To illustrate how using the 2-μm band could improve the limited operability of device-independent (DI) QKD at daytime, we model the secure key rate using the results in Refs. [15,22] as a function of detection efficiency versus the number of photons per pulse, at different carrier wavelengths by using the solar flux densities with a 100-nm band around the carrier wavelengths. Figure 1 shows a significant parameter region in which positive secure key rates that are unachievable
FIG. 1. Comparison of the lower bounds on the secure key rates $R$ for DIQKD as functions of the number of photons per pulse $\mu$ and total channel efficiency $\eta$ at 2.1, 1.55 $\mu$m and 770 nm simulated based on solar photon flux density data at sea level and infrared atmospheric transmission spectrum in Ref [21]. This simulation is based on the theoretical results in Refs. [15,22] and solar background flux measured in Ref. [29].

at 1.55 $\mu$m and 770 nm become achievable at 2.1 $\mu$m. In addition, an entangled photon source has been developed [23] and low noise superconducting photon counting detectors have become available [24] at approximately 2 $\mu$m, opening up this spectral window for quantum optics and quantum communications.

The main approaches for implementing QKD are based on the Bennet-and-Brassard (BB84) and the Ekert91 protocols [25,26]. In both cases, an important metric is the quantum bit error rate (QBER), i.e., the ratio of wrong bits to the total number of transmitted bits, and it contains information about the existence of an eavesdropper and how much they may know. Entanglement-based quantum information protocols approach optimal performance when the resource state is known, and in particular, when it approaches a maximally entangled state. For DIQKD, the resource state must demonstrate a combination of low QBER and sufficiently large Bell inequality violation to yield a positive (i.e., greater-than-zero) secure key rate [15]. Previously, quantum interference and polarization entanglement in free space with Clauser-Horne-Shimony-Holt (CHSH)-Bell inequality violation by 2.2 standard deviations [23] and quantum interference with heralded single photons on chip [27] was demonstrated in the 2-$\mu$m band. However, the capability for general projective measurements and full characterization of single and entangled qubit states in the midinfrared region has not previously been demonstrated. These capabilities are crucial for the implementation of advanced quantum information tasks. Moreover, a positive secure key rate, which demonstrates the viability of entanglement-based QKD protocols, has not yet been shown.

Results and discussion.—In this work, we demonstrate quantum state tomography of two-photon states in the mid-infrared spectral region, and show near-maximal entanglement through violation of the CHSH-Bell inequality with more than a ninefold improvement over previous experiments, in terms of the number of standard deviations above the classical bound [23]. Most importantly, we give an experimental demonstration of a state corresponding to a positive secure key rate in the midinfrared region in a DIQKD setting. We have shown that our source is capable of violating a Bell inequality for which a weak form of self-testing has recently been proven [28]. This type of self-testing allows the certification of the entangled state without certifying the implemented measurements. This is of fundamental interest since, previously, self-testing of quantum states or randomness certification had only been shown for rigid Bell inequalities.

We generate the photon pairs using spontaneous parametric down-conversion (SPDC) in a second-order nonlinear crystal with a configuration similar to that in our previous work [23]. As illustrated in Fig. 2, the nonlinear crystal is pumped with a ytterbium-based ultrashort-pulse fiber laser (Chromacity Ltd.) at a carrier wavelength of approximately 1040 nm, a repetition rate of 80 MHz, and a pulse duration of 130 fs. Here, we use periodically poled, magnesium-doped lithium niobate crystals (MgOPPLN; Covesion Ltd.) with lengths 1 and 0.3 mm cut for type-0 and type-2 phase matching, respectively. The crystals are fabricated with different poling periods that are tested at different temperatures to determine the configuration that maximizes the signal and idler photon count.

FIG. 2. Experimental setup for generation and full tomography of polarization entangled photons at 2.1 $\mu$m. The setup consists of mirrors ($M_1/2$), an energy controller (EC), lenses ($L_1$ and FC1/2), the periodically poled lithium niobate (PPLN) crystal ($C$), Ge filter ($F_0$), a D-shaped pickoff mirror ($D$), 50-nm-passband filters ($F_{1/2}$), halfwave plates ($H_{1/2}$), quarterwave plates ($Q_{1/2}$), polarizers ($P_{1/2}$), single-mode fibers (SMF1/2), and superconducting nanowire single-photon detectors (SNSPD1/2).
rates in each case. The optimal specifications are a poling period of 31.4 $\mu$m (9.486 $\mu$m) and a stable temperature of 90 $\pm$ 0.1 °C (150 $\pm$ 0.1 °C) for the type-0(2) crystal.

For the type-0 experiment, where the polarization of the pump photon is the same as that of the daughter photons, we pump with vertically polarized photons $|V\rangle_p$ to obtain the separable two-photon state $|V\rangle_1 \otimes |V\rangle_2$ at 2080 nm, where “$\otimes$” denotes the tensor product, and we use $|X\rangle_0 \otimes |Y\rangle_1 \equiv |X, Y\rangle$ in what follows. On the other hand, in the type-2 configuration, we pump with horizontally polarized photons $|H\rangle$ to obtain the entangled two-photon singlet state $|\psi^-\rangle = (1/\sqrt{2})(|H\rangle _0 \otimes |V\rangle _2 - |V\rangle _0 \otimes |H\rangle _2)$ at 2080 nm. As illustrated in Fig. 2, the output of the crystal is then recollimated using a parabolic mirror and passed through an antireflection-coated germanium long-pass filter, $F0$ (cut on approximately 1.85 $\mu$m), to reject the intense laser excitation light, thereby ensuring the purity of the measured state. Also, the photons are further filtered using 50-nm bandpass filters, $F1$ and $F2$, in each arm to select the degenerate SPDC photon pairs at 2080 nm before final detection. After the long-pass filter, the signal and idler photons are separated in the far field using a D-shaped pickoff mirror, $D1$. The signal (idler) photons are then passed through a quarterwave plate, $Q1$ ($Q2$); a halfwave plate, $H1$ ($H2$); and a fixed horizontal polarizer $P1$ ($P2$). This allowed projection onto any general polarization basis state. Such access to the entire Hilbert space is required for general projective measurements, and in particular for full quantum state tomography. Finally, a lens (18.4-mm focal length) coupled the photons in each arm into a single-mode fiber (SM2000), which in turn coupled the photons to high-efficiency superconducting nanowire single-photon detectors (SNSPD; single quantum).

To give insight on the pumping conditions for the optimum trade-off between the count rates and the state purity, we perform measurements of the coincidence-to-accidental ratio (CAR) at various pump powers, as shown in Figs. 3(a) and 3(b). For the type-0 case, we project the state onto $|V, V\rangle$ and measure a maximum CAR of 607 $\pm$ 185, which is approximately 3 times the state of the art. This improvement is in part due to the use of SNSPDs with higher efficiencies. Similarly, for the type-2 crystal, by projecting the entangled state to the $|H, V\rangle$, we measure CAR up to 354 $\pm$ 127 (projection onto $|V, H\rangle$ gives identical results). By fitting a standard model [23,30] to the data as done in Ref. [23], we estimate the lumped efficiencies as $\eta_1 \simeq \eta_2 = 2.26 \pm 0.03%$.

We perform full quantum state tomography [31] on the two-photon states in the type-0 and type-2 configurations (see Sec. SI within the Supplemental Material [32]). Because of the higher-photon fluxes (see Fig. 3), the type-0 experiments facilitated the calibration of the measurement setup in preparation for measuring and characterizing the entanglement of type-2-generated photon pairs. Figures 4(a) and 4(b) show the results of the reconstructed density matrix. These are measured with 20- and 30-min integration times, and coincidence rates of 13.92 and 1.2 Hz for the type-0 and type-2 sources, respectively. The highest-fidelity pure state corresponding to the reconstructed density matrix for each case is

$$|\psi\rangle_0^{\text{exp}} \simeq 0.99|V, V\rangle + (0.10 + 0.03i)|H, H\rangle$$

and

$$|\psi\rangle_2^{\text{exp}} \simeq -0.02|V, V\rangle + (0.59 - 0.06i)|V, H\rangle + (-0.8 + 0.08i)|H, V\rangle + 0.02|H, H\rangle$$

for type-0 and type-2 SPDCs, respectively. The fidelities [33] of the reconstructed density matrices with the ideal $|V, V\rangle$ and $|\psi^-\rangle$ states are $F_0 = 99.25\%$ and $F_2 = 89.54\%$, while the state purities $[P_{0(2)} = \text{Tr}(\rho_{0(2)}^2)]$ are $P_0 = 98.54\%$ and $P_2 = 84.57\%$ for type 0 and type 2, respectively.

While an entangled state was achieved previously [23], a state sufficiently entangled to result in a positive secure key rate for DIQKD has not been demonstrated. To evaluate the suitability of our source for quantum information and
We also determine the QBERs in the $Z$ and $X$ bases as
\[
E_Z = \text{Tr}(\rho|H,H\rangle\langle H,H|) + \text{Tr}(\rho|V,V\rangle\langle V,V|),
E_X = \text{Tr}(\rho|+,+\rangle\langle +,+|) + \text{Tr}(\rho|-,+\rangle\langle +,-|)
\]
(2)
to be 6.89% and 3.80%, respectively, where $|\pm\rangle = (|H\rangle \pm |V\rangle)/\sqrt{2}$. Using Eq. (1), these give lower bounds $R$ on the secure key rate as 0.126 and 0.254 bits/pair, respectively. Based on a coincidence detection rate of 1.2 Hz, these correspond to 0.15 and 0.3 secure bits/s, respectively. The finite lower bound of 0.254 secure bits per detected pair seems promising for a demonstration in the 2.1-$\mu$m waveband, albeit in a proof-of-principle scenario under the fair sampling assumption, and in a laboratory setting (an approximately 2-m transmission distance). We expect to be able to increase the photon-pair rate by exploiting higher SPDC generation efficiencies with a longer PPLN crystal along with longer-pulse or continuous-wave (CW) pumping. Also, since type-0 and type-1 SPDC generation typically have higher efficiencies, these could also be employed in a Sagnac configuration as done in Ref [11] to generate high-quality entangled states at higher fluxes. Recent theoretical work [40] on high-purity photon pair generation using bulk potassium niobite (KNbO3, KN), suggesting the possibility for signal-idler generation at 2128 nm with higher efficiencies than type-2 PPLN crystals, provides yet another promising route.

Using the results of from Ref. [41], we obtain a lower bound on the entanglement present in the state as measured by entanglement of formation and concurrence [42] of $E_F = 0.818425$ and $C = 0.8712$, respectively. These are widely studied measures of entanglement of a general bipartite quantum system, which increase monotonically with the degree of entanglement in the state. The concurrence is 0 for a separable state and 1 for a maximally entangled state. We note here that these conclusions rely on the assumption that the state being measured is a two-qubit state; hence, they are not fully DI. A fully DI conclusion that certifies that the state can be locally processed to obtain a state that approaches a singlet state can be obtained using the results in Ref. [43]. In fact, the threshold violation for which the self-testing bound becomes nontrivial is $S^* = (16 + 14\sqrt{2}/17) ≈ 2.11$, and with $S = 2.531 > S^*$ in Eq. (7) of Ref [43], we can guarantee that, up to local operations, the lower bound on the singlet fidelity is 79.4%, demonstrating a fully DI certification of the two-photon state generated at 2.1 $\mu$m.

We further exploit the quality of the entangled state and the measurement capabilities to demonstrate a previously unexplored quantum application—a weak form of self-testing recently derived in Ref. [28]. Self-testing [44–46] is a means for DI characterization of quantum devices by a classical user solely on the basis of observed nonlocal correlations, without requiring any assumptions about the devices under test [47]. Traditionally, this is based on the
violation of so-called “rigid” [48] Bell inequalities such as the CHSH. Self-testing with such inequalities is rigid in the sense that it certifies both the quantum state measured and the measurement implemented by the device. The weak form of self-testing [28], which has not yet been addressed experimentally, now makes it possible to certify the quantum state without full determination of the measurements. Based on the violation of the three-setting inequality (see Sec. SIII within the Supplemental Material [32]), we demonstrate that we have a two-qubit state that exhibits a violation of the $\alpha = 1$ inequality of 4.5388 (local bound is 4). This allows us to conclude that no pair of observables used in the experiment commute (i.e., we have a fully nontrivial incompatibility structure).

Conclusion.—We have demonstrated how quantum technologies in the midinfrared region have now reached the maturity level that enables the generation, manipulation, and full tomography of highly entangled quantum states. We have confirmed that this state could be used for DI randomness generation or quantum key distribution (or possibly other cryptographic tasks), and as examples, we have computed the secure key rate for DIQKD. This represents a significant step towards DI quantum information and communication protocols in this waveband. For example, DIQKD during daytime could be realized by harnessing the low solar background within the 2.1-$\mu$m window. Key milestones that are yet to be achieved in this waveband include the development of near-unity efficiency single-photon detectors, as now available at telecom wavelengths [49].

Together with recently developed techniques for satellite-to-ground entanglement distribution and QKD [9,10], our approach could lead to the future development of metropolitan quantum networks. Moreover, the recent development of HCFs [18,20,50], on chip components for light generation and manipulation [27], and gigahertz-bandwidth switching devices in the 2-μm band [51] suggest the 2-μm band as one that will support interconnectivity between the guided-wave, integrated, and free-space platforms, which could further extend the applicability in future full-scale DIQKD implementations, and allow distribution of entangled photons over large distances between nodes through fiber optic networks. Our results further lay the foundations for advanced quantum technologies in the midinfrared spectral region.

All the data supporting the conclusions reported in this manuscript are available online [52].

Acknowledgments.—A.C.D. acknowledges support from the EPSRC, Impact Acceleration Account (EP/R511705/1). M.C. and A.C.D. acknowledge support from the UK Research and Innovation (UKRI) and the UK Engineering and Physical Sciences Research Council (EPSRC) Fellowship (“In-Tempo” EP/S001573/1). J.K. acknowledges support from the project “Robust certification of quantum devices” carried out within the HOMING programme of the Foundation for Polish Science cofinanced by the European Union under the European Regional Development Fund. R.H.H. acknowledges support from the EPSRC Quantum Communications hub EP/T001011/1. D.F. is supported by the Royal Academy of Engineering under the Chairs in Emerging Technologies scheme.


[27] L. M. Rosenfeld, D. A. Sulway, G. F. Sinclair, V. Anant, J. Kaniewski, Analytic and Nearly Optimal Self-Testing of entanglement (Sec. SIII), and the calculation of the measures of entanglement (Sec. SIV).


[47] See Supplemental Material at http://link.aps.org/supplemental/10.1103/PhysRevApplied.16.L051005 for more details on the density matrix reconstruction (Sec. SI), the determination of the theoretical maximum of the Bell parameter (Sec. SIII), and the calculation of the measures of entanglement (Sec. SIV).